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G. G. Bunatian*, V. G. Nikolenko, A. B. Popov

ON THE USAGE OF ELECTRON BEAM AS A TOOL TO PRODUCE RADIOACTIVE ISOTOPES IN PHOTONUCLEAR REACTIONS

^{*}E-mail: bunat@cv.jinr.dubna.ru

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Бунатян Г. Г., Николенко В. Г., Попов А. Б. Использование потока электронов для производства радиоактивных изотопов посредством фотоядерных реакций

Исследуются тормозное излучение, которое порождается исходным потоком электронов в конвертере, и производство требуемого радиоизотопа благодаря фотоядерным реакциям, обусловленным этим тормозным излучением. Представлены, в качестве иллюстрации, численные расчеты выхода ряда радиоизотопов, имеющих наибольшее практическое применение. Результаты исследований убеждают нас в том, что использование современных ускорителей электронов дает реальную возможность для производства радиоизотопов в количествах, необходимых в настоящее время для разнообразных применений, представляющих большую ценность, в ядерной медицине.

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Bunatian G. G., Nikolenko V. G., Popov A. B.E6-2009-182On the Usage of Electron Beam as a Toolto Produce Radioactive Isotopes in Photonuclear Reactions

We treat the bremsstrahlung, induced by initial electron beam in converter, and the production of a desirable radioisotope due to the photonuclear reaction caused by this bremsstrahlung. By way of illustration, the yield of a number of some, the most applicable in practice, radioisotopes is evaluated. The acquired findings persuade us that usage of modern electron accelerators offers a practicable way to produce the radioisotopes needful nowadays for various valuable applications in the nuclear medicine.

The investigation has been performed at the Frank Laboratory of Neutron Physics, JINR.

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INTRODUCTION

Nowadays, it is rather impossible to find any branch of science, industry, medicine, forensic, asf, in which the radioisotopes are not widely used [1–6]. Although there is a series of unstable natural isotopes arising from the decay of primordial uranium and thorium, the most of about 200 radioisotopes used for now on a regular basis are produced artificially. Despite all the nuclear reactors produce the manifold radioisotopes as a result of fission of 235 U contained in their fuels, the recovery of these radioisotopes is extremely problematic issue, and they would not be received for primary applications, especially for medical use.

At present, radioisotope marketable production is primarily brought about by exposition of the appropriate element to neutrons in a nuclear reactor, or to charged particles, like protons, deuterons, or alpha particles, in a cyclotron [7]. As a general rule, it is far more difficult to make a radioisotope in a cyclotron than in a reactor. Cyclotron nuclear reactions are less productive and less predictable than ones performed in a reactor. The variety of cyclotron-produced radioisotopes is tightly restricted, too. Economic factors would also militate against cyclotron production. In fact, it proves to be anyway not competitive with the reactor radioisotope production.

As to reactor-based manufacturing, there are two processes to produce isotopes: fission of ²³⁵U by neutrons within an exposed target, with subsequent recovery of a desirable isotope out of fission fragments, and neutron capture by nucleus of an appropriate sample, which results in elaboration of a required isotope [7]. The ²³⁵U fission cross section σ_{nf} is well known to be at least a factor of about 100 greater than the typical neutron capture $A(Z, N)(n, \gamma)A'(Z, N+1)$ cross section to produce some radioisotope A'(Z, N+1) that could otherways be recovered from ²³⁵U fission fragments. That is why the radioisotope consumers community world-wide dismissed the neutron capture as a viable process for production of the primary needful radioisotopes in quantities required to meet global demand, thought this process could be used to make minor radioisotope amounts to provide a stable domestic supply. For instance, in Russia different radioisotopes, including ⁹⁹Mo/^{99m}Tc, are produced on the Leningrad power station using the neutron capture reactions in the channel of the RBMK-1000 reactor [8]. Thus, in these days, the most of the world's production of primary radioisotopes is carried out by irradiating highly enriched uranium (HEU) targets in research and test reactors that provide a thermal neutron flux $(10^{14}-10^{15})$ n/ (s \cdot cm²), and are fueled with low enriched uranium (LEU), or in some cases with (HEU) as well [7]. These reactors have become indispensable for the industrial production of marketable radioisotopes, in particular, medical isotopes, to supply the rapidly increasing demand for diagnostic and therapeutic procedures based on nuclear medicine techniques. The nuclear-medicine community defines the medical isotopes to include first of all the isotope ⁹⁹Mo, that is the precursor to the short-living ^{99m}Tc that is used in $\approx 85\%$ of all the nuclear medicine procedures worldwide, and also ¹³¹I, ¹³³X and other manifold radioactive materials used to produce radiopharmaceutics [2, 4, 7, 9, 10]. The medical radioisotope recovery is humanly the most vital outcome of nuclear physics and industry.

The supply reliability of radiopharmacies, hospitals, clinics, and outpatients centers with the radioisotopes is currently the primary concern of the world nuclear-medicine community [7]. In actual fact, recent experience suggests that unplanned emergent reactor shutdowns would cause severe supply disruption. A number of contingence incidents during last years has been pointing up unreliability in the supply of medical radioisotopes, in particular ⁹⁹Mo/^{99m}Tc. Some 95% of the world's supply of these comes from only five reactors, all of them are over 40 years old [7]. So the greatest single threat to supply reliability is the approaching obsolescence of the aging reactors that current large-scale producers utilize to irradiate HEU targets to elaborate the needful radioisotopes. Last years, there took place a number of significant disruptions in medical radioisotope supply, some of which have been lasting by now [7,11]. For instance, the concern about the long-term supply of medical radioisotopes has been exacerbated when the shutdown of research reactor HFR in the Netherlands since August 2008 has caused ⁹⁹Mo shortage world-wide. The most productive and oldest, yet a while ago refurbished, Canada's NRU reactor was shutdown last summer 2009 [12], after the heavy water leak was discovered in May 15, 2009. It is not clear if and when the NRU could be restarted, or how to make up for its outage. The worldwide supply of radioisotopes is likely to be unreliable unless newer production sources come on line.

Besides posing a threat to patients treatment, the current method used by the world's main producers increases the menace of nuclear terrorism, as it employs weapons-grade HEU. So the burning question is now to eliminate, or at least minimize, the HEU use in reactor fuel, irradiated targets, and production facilities. Only very few small-scale producers, e.g., in Argentina and Australia, are, or are going to be able to manufacture radioisotopes using the LEU targets [7]. The bulk of consumed radioisotopes are still obtained utilizing HEU and, to the best of knowledge, the conversion to the LEU targets is not believed before long. Especially the radioisotope producing community had been counting on the to-

be-built reactors MAPLE1 and MAPLE2, and on the related processing facilities at Chalk-River site, Canada, which would not have used the HEU. Yet, the MAPLEs, designed as a replacement for NRU, did not perform as contemplated, and in May 2008 Atomic Energy of Canada Ltd. made the decision to end the MAPLE's project [13]. This has, in fact, put on hold any plans to convert to LEU-based large-scale radioisotope production. Instead, the world community these days needs both the new radioisotope production inventions and the facilities that will continue work safely in the long term, without using weapon-grade uranium.

In this respect, we treat in what follows the photoproduction of various radioisotopes (Secs. 2, 3) which is due to the bremsstrahlung induced in converter by initial electron beam of electron accelerator, Sec. 1. Also we consider, in Sec. 4, the case when a desirable isotope results in decaying a parent radioisotope that stems itself in the photoproduction. At last, in Sec. 5, the all-round discussion of findings persuades us that the most preferable way to produce radioisotopes is the usage of electron beams provided by modern electron accelerators. What encourages our work is the exploration by now carried out in [14–17].

1. BREMSSTRAHLUNG IN CONVERTER

As was proclaimed above, the purpose is to acquire how to work out the various radioisotopes, needful to-day for manifold applications in technology, science, and medicine, by making use of electron beams delivered by microtrons, linear electron accelerators, etc. That beam, with an electron energy distribution $\rho_e(E_e)$ and a current density $J_e(t)[A/cm^2]$ (generally speaking, time-dependent), travels through the converter (see Fig. 1), which is prepared of some proper heavy element, such as W, Pt, etc. The bremsstrahlung is thereby induced with current density

$$J_{\gamma}(E_{\gamma}) = \frac{\mathcal{N}_{\gamma}(E_{\gamma})}{\mathrm{s} \cdot \mathrm{cm}^2 \cdot \mathrm{MeV}},$$
(1.1)

expressed in terms of the photon number $\mathcal{N}_{\gamma}(E_{\gamma})$ with the energy $E_{\gamma} = |\mathbf{k}| = k$, per 1 cm², 1 s, 1 MeV.

In turn, that γ -ray flux, interacting with respective nuclei of the sample (see Fig. 1), induces the photonuclear reaction

$$\gamma + A(Z, N) \Longrightarrow A'(Z, N-1) + n, \tag{1.2}$$

so that a desirable isotope A'(Z, N-1) comes out. Certainly, this process (1.2) can only be realized if the energy E_{γ} of γ rays is, at least, greater than the neutron binding energy B_n of a considered nucleus $A(Z, N), E_{\gamma} > B_n \approx 8$ MeV. Actually, the isotope A(Z, N-1) production process will successfully run provided E_{γ} is of the order of, and comes over the energy E_{GR} of giant resonance in the photonuclear reactions (1.2) on respective nuclei, $E_{\gamma} \gtrsim E_{GR}(Z, N) \sim 13-19$ MeV [18].

As a matter of course, an electron must have got the energy $E_e > E_{\gamma}$ in order to give rise to the bremsstrahlung with the required energy E_{γ} .

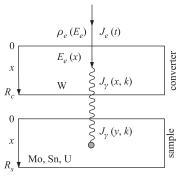


Fig. 1. The setup scheme

Thus, only the processes involving the electron and photon energies

$$E_{\gamma}, E_e \gtrsim E_{GR}$$
 (1.3)

are to be taken into consideration and explored, which is the key point of our treatment. Next, we limit the current study by the condition

$$E_e \leqslant 100 \text{ MeV}$$
 (1.4)

as well. The guide relations (1.3), (1.4) govern all the presented calculations, specifying the energy area where the acquired findings hold true. Also, in the ordinary way, all the evaluations

we make in the work are the first α -order, and we abandon contributions from all the high α -order processes.

In passing across converter, a high-energy electron is primarily known to lose its energy (see, e.c., [19–21]) due to the bremsstrahlung by scattering in the fields of nuclei of heavy atoms of converter. As the relation (1.3) holds, the angular distribution of scattered electrons as well as emitted photons has got a sharp maximum in momentum direction of an initial electron. Both electrons and photons spread within a small, rather negligible solid angle $\Theta \sim m/E_e$ around direction of the initial electron momentum [19–21]. Then, with proper allowance for screening, upon integrating the bremsstrahlung cross section over the angle between the momenta of incident electron and emitted photon, a very handy expression for the cross section to describe the photon energy distribution results in (see, e.g., [20, 22, 23]):

$$\frac{\mathrm{d}\sigma_b(k)}{\mathrm{d}k} = \frac{2Z_C^2}{137} r_0^2 \frac{1}{k} \cdot \left\{ \left(\frac{E_e^2 + E_e'^2}{E_e^2} - \frac{2E_e'}{3E_e} \right) \cdot \left(\ln M + 1 - \frac{2}{b} \arctan b \right) + \frac{E_e'}{E_e} \left(\frac{2}{b^2} \ln(1+b^2) + \frac{4(2-b^2)}{3b^3} \arctan b - \frac{8}{3b^2} + \frac{2}{9} \right) \right\}, \quad (1.5)$$

where $k = E_{\gamma}$ stands for the energy of radiated γ quantum, $E'_e = E_e - k$, Z_C is the atomic number of the converter material, and

$$b = \frac{2E_e E'_E Z^{1/3}}{C m k}, \quad \frac{1}{M} = \left(\frac{m k}{2E_e E'_e}\right)^2 + \frac{Z_C^{2/3}}{C^2}$$
$$C = 111, \quad r_0 = \frac{e^2}{m} = 2.818 \cdot 10^{-13} \text{ cm}.$$

Besides the aforesaid bremsstrahlung in the field of nucleus, there exists the bremsstrahlung by scattering an incident electron by atomic electrons. For a fast electron, $E_e \gg m$, the cross section of this process is known to coincide with the bremsstrahlung cross section on nucleus with Z = 1 [19–21]. Then, the atomic electrons contribution into the whole electron bremsstrahlung is taken into account just by replacing the factor Z_C^2 in Eq. (1.5) by $Z_C(Z_C + \delta)$ with $\delta \lesssim 1$. As for heavy converter atoms $Z_C \gg 1$, this correction is rather of very small value.

The bremsstrahlung, with all the feasible energies $k = E_{\gamma}$, causes the mean energy loss of electron on a unit of path [19,20]

$$-\frac{\mathrm{d}E_e(x)}{\mathrm{d}x} = \mathcal{N}_C E_e(x)\varphi_{\mathrm{rad}}(E_e). \tag{1.6}$$

The number \mathcal{N}_C of scattering atoms of converter in 1 cm³ is

$$\mathcal{N}_C = \frac{\rho_C \cdot 6.022 \cdot 10^{23}}{A_C},\tag{1.7}$$

where ρ_C is the density of converter material, and A_C is its atomic weight. The quantity φ_{rad} is written in the form

$$\varphi_{rad} = \bar{\varphi} \cdot K_C(E_e) = K_C(E_e) Z_C^2 \cdot 5.795 \cdot 10^{-28} \text{ cm}^2.$$
(1.8)

The coefficient K_c , very slightly varying with the energy E_e , provided $E_e \gtrsim 10$ MeV, can be found in [19,20,24] for various heavy atoms. So, upon passing a path x, an electron with initial energy $E_e(0)$ will have got, in consequence of the radiative losses, the energy

$$E_{e \ rad}(x) \approx E_e(0) \exp[-x \mathcal{N}_C \varphi_{\rm rad}].$$
 (1.9)

In fast electrons, $E_e \gg m$, elastic scattering on heavy nuclei of converter, the angular distribution has got a very sharp maximum, within the solid angle $\Theta < (m/E_e)^2$, and therefore can be left out of our consideration [19–21].

In treating the fast electron collision with atomic electrons, without photon emitting, we are to consider two cases. Firstly, let the momentum Δ_I transferred to an atomic electron be

$$\Delta_I \lesssim I_Z \approx 13.5 Z_C \text{eV},\tag{1.10}$$

 I_z being the ionization potential of atom. Apparently, as $\Delta_I \ll E_e$, a scattering angle is negligible. The mean electron energy loss on a unit of path, caused by its inelastic collisions with atoms, is described by the expression (see [19,20,23])

$$-\frac{\mathrm{d}E_e(x)}{\mathrm{d}x} = 2\pi r_0^2 m \mathcal{N}_C \, Z_C \ln \frac{E_e^3(x)}{2m I_Z^2},\tag{1.11}$$

which can be rewritten in the form

$$x = -\frac{1}{6\pi r_0^2 m \mathcal{N}_C Z_C} \int_{E_e(0)}^{E_{eI}(x)} \frac{\mathrm{d}E}{\ln[E(2mI_Z^2)^{-1/3}]},$$
(1.12)

where $E_e(0)$ is the electron energy at the starting edge of converter, and $E_{eI}(x)$ stands for the electron energy upon passing the distance x, which is caused by the ionization losses. With the conditions (1.3), (1.4), we can actually presume

$$\ln E \approx \ln E_e^{av}, \quad E_e^{av} = \frac{E_e(0) + E_{GR}}{2}$$
 (1.13)

in Eq. (1.12). Then we arrive at the estimation of the energy loss on the distance x due to the inelastic electron collisions with atoms

$$\Delta E_{e\,I}(x) \approx -x6\pi r_0^2 m \mathcal{N}_C Z_C \ln[E_e^{av} (2mI_Z^2)^{-1/3}].$$
(1.14)

Secondly, when, unlike (1.10), the momentum transferred $\Delta_I \gg I_Z$, yet still $\Delta_I \ll E_e$ anyway, atomic electrons can be considered as free ones, and the fast electron interaction with them reduces to the elastic forward scattering on free resting electrons [19, 21], which causes, as a matter of fact, no energy loss.

Amenably to Eqs. (1.9), (1.12)–(1.14), the electron with the incident energy $E_e(0)$ at the starting edge of converter has got the energy

$$E_e(x) \approx E_{e \operatorname{rad}}(x) - \frac{6\pi r_0^2 m Z_C \ln[E_e^{av} (2m I_Z^2)^{-1/3}]}{\varphi_{rad}} \left(1 - \frac{E_{e \operatorname{rad}}(x)}{E_e(0)}\right) \approx \\ \approx E_{e \operatorname{rad}}(x) + \Delta E_{e I}(x), \quad (1.15)$$

upon passing the path x through converter (see Fig. 1). Just this, x-dependent, energy $E_e(x)$ is to be substituted into Eq. (1.5) to describe the bremsstrahlung of an electron at the distance x from the starting edge of converter. Thus, the bremsstrahlung production cross section (1.5) turns out to be the function of the distance x, via the electron energy $E_e(x)$ (1.15).

In the actual evaluation explicated further in Secs. 2, 3, the converter thickness R_C proves to be chosen so that there are no electrons with the energies $E_e(R_C) \gtrsim 10 \text{ MeV} \gg m$ at the final edge of converter.

As expounded above, only the bremsstrahlung with $k \gtrsim 10 \text{ MeV} \gg m$, described by Eq. (1.5), is of value to induce the desirable photonuclear reaction (1.2). This bremsstrahlung, caused by the initial electron beam with the energy distribution $\rho_e(E_e)$ and the current density $J_e(t)$, when stems at a distance x from the starting edge of converter, is described by the photon current density (1.1)

$$J_{\gamma}(x,k,E_e,Z_C,\rho_C,t) = \rho_e(E_e)J_e(t)\mathcal{N}_C\frac{\mathrm{d}\sigma_b(k,E_e(x),Z_C)}{\mathrm{d}k},\qquad(1.16)$$

where the cross section $d\sigma_b/dk$ is given by Eq. (1.5) with the electron energy $E_e(x)$ (1.15). This γ flux spreads then forward, as was explicated above.

In this bremsstrahlung passing the path $(R_C - x)$ from a point x up to the final edge of converter R_C (see Fig. 1), there are three processes which cause the continuing γ -ray absorption [19–21]: 1) the e^+e^- -pairs production; 2) the photoeffect; 3) the Compton scattering on electrons; the first one is known to be of the crucial importance at the considered $k \gtrsim 10$ MeV [19–21]. Consequently, the bremsstrahlung current density $J_{\gamma}(x,k)$ (1.16) decreases, becoming at the final edge of converter

$$J_{\gamma}(x,k,R_C) = J_{\gamma}(x,k) \cdot \exp\left(-\frac{R_C - x}{l_C(Z_C,\mathcal{N}_C,k,\rho_C)}\right),\tag{1.17}$$

where the length of absorption l consists of three aforesaid parts

$$\frac{1}{l_C} = \frac{1}{l_{\text{pair}}} + \frac{1}{l_{\text{photo}}} + \frac{1}{l_{\text{Com}}}.$$
(1.18)

Generally speaking, a tiny small quantity $1/l_{\gamma n}$, caused by the reactions like (1.2), should have been added to right-hand side of Eq. (1.18), for the conscience's sake. The values of l for various materials are found, for instance, in [20, 24]. Let us mention that we deal with the γ -ray energies just above the so-called «area of maximum transparency» [19, 20, 24].

As understood, precision of all the carried out calculations is proved to be at least of the order $\sim m/E_{GR}$, $\sim I_Z/E_{GR}$, that is anyway none the worse than $\sim 10\%$.

With taken into consideration the restrictions imposed by the guide conditions (1.3), (1.4), we shall now discuss how the cascade of electrons and photons, practicable to the isotope production (1.2), would emerge. The processes in those an electron with the energy $E_e < E_{GR}$ participates cannot anyway lead to any discernible contribution into the photoneutron production (1.2) of the desired isotope A'(Z, N-1). In slowing-down from the initial energy $E_e(0)$ to the energy E_{GR} , an electron loses the energy

$$\hat{\Delta} \approx E_e(0) - E_{GR}.$$
(1.19)

This energy loss $\tilde{\Delta}$ itself is not considered to be small. So, at the maxima currently treated electron energy $E_e(0) = 100$ MeV, we would have got $\tilde{\Delta} \approx 85$ MeV, and for the timely most vital $E_e(0) = 50$ MeV we would arrive at $\tilde{\Delta} \approx 35$ MeV. As generally received [20, 25], the primary share of this energy loss $\tilde{\Delta}$ is radiated most probably as the γ rays with energies

$$\tilde{k} = \tilde{E}\gamma \approx \frac{\dot{\Delta}}{2}.$$
 (1.20)

Only a small part of this energy loss $\tilde{\Delta}$ is emitted as a flux of comparatively soft photons, and γ radiating with the energies $k = E_{\gamma} > \tilde{k}$ proves to be all the more

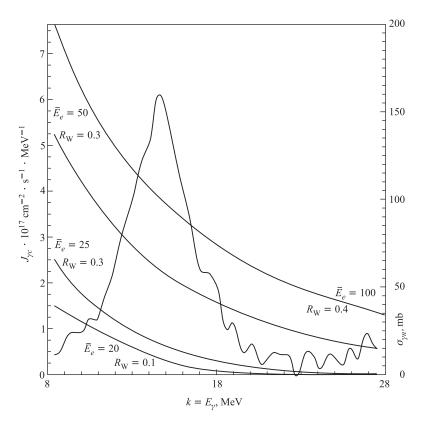


Fig. 2. The dashed curves represent the k dependence of the γ flux (1.22) at the final edge of converter for various $\bar{E}_e(\text{MeV})$ and the most preferable thicknesses $R_W(\text{cm})$, which are plotted alongside the respective curves. The electron energies are distributed around the given $\bar{E}_e(\text{MeV})$ according to Eq. (1.23) with the E_e^b , E_e^u , Δ_e values chosen as in Table 5. The initial electron current density $J_e = 1 \text{ A/cm}^2$. The solid curve represents k dependence of the cross section of reaction in Eq. (3.1)

negligible [20,25]. As was already discussed above, in absorbing a photon with the considerable energy \tilde{k} (1.20), the e^+e^- pairs are produced with approximately equal energies

$$E^+ \approx E^- \approx \frac{\dot{k}}{2} \approx \frac{\dot{\Delta}}{4}.$$
 (1.21)

Surely, there is no reason to suggest these energies to be as small as negligible, yet anyway they are nevertheless substantially smaller than the initial electron energy $E_e(0)$. Thus, for the timely most vital case $E_e(0) = 50$ MeV, we have got $E^{\pm} \approx 8$ MeV $< E_{GR}$, so that the thereby produced e^+, e^- can never contribute to the isotope production (1.2) at all, which is understood in observing Fig.2.

Put another way, there would be a cascade, but the particles participating therein would have got energies beyond the key condition (1.3). At the largest initial electron energy we currently consider (1.4), $E_e(0) = 100$ MeV, there would be $E^{\pm} \approx 20$ MeV, so as, generally speaking, these e^+, e^- themselves would give rise to the bremsstrahlung which could in turn serve to the isotope A'(Z, N-1) photoneutron production (1.2). Yet this isotope production, caused by those secondary electrons with energies $E^{\pm} \approx 20$ MeV, is anyway 10 times as small as the production due to the initial electrons with $E_e(0) = 100$ MeV themselves, which comes to light in observing the findings presented in Tables 5, 6, 7, Sec. 3. Thus, when we abandon, even at $E_e(0) = 100$ MeV, the above explicated cascade, the thereby inherent ambiguities will never come over $\approx 10\%$. That is why we do not draw into consideration the bremsstrahlung which would be induced, in converter or in sample, by the electrons that themselves would be originated by absorption of the bremsstrahlung, which in its turn is due to the scattering of an initial electron on nuclei in converter.

Upon integrating Eq. (1.17) over the initial electron energy distribution and over the converter length, we obtain the bremsstrahlung flux at the final edge of converter

$$J_{\gamma C}(k, R_C, Z_C, \rho_C, E_E^b, E_e^u, \Delta_e, t) = \\ = \int_{E_e^b}^{E_e^u} dE \rho_e(E) \int_{0}^{R_C} dx J_{\gamma}(x, k, R_C, E, Z_C, \rho_C, t), \quad (1.22)$$

where E_e^b, E_e^u are, respectively, the bottom and upper energies of the electron distribution in the beam, and Δ_e is to describe its width. In our further actual evaluations, the electron energy varies between the limits E_e^b, E_e^u , and we choose

$$\rho_e(E) = \frac{1}{n} \exp[-((E - \bar{E})/\Delta_e)^2], \ \bar{E} = \frac{E_e^b + E_e^u}{2}, \ n = \int_{E_e^b}^{E_e^u} dE \rho_e(E). \ (1.23)$$

Surely, when $\Delta_e \rightarrow 0$, Eq. (1.23) reduces to the δ -function electron energy distribution. Also, let us recall the initial electron current density J_e in Eqs.(1.16), (1.17), (1.22) is given in A/cm² = $10^{19} \text{e}^{-}/(1.602 \cdot \text{s} \cdot \text{cm}^2)$, where e⁻ is the electron electric charge.

2. RADIOISOTOPE PHOTOPRODUCTION IN SAMPLE

Traveling forward, the bremsstrahlung flux (1.22) intrudes into the sample (see Fig. 1) that incorporates the isotope A(Z, N) which serves to produce the desirable radioisotope A'(Z, N - 1) due to the photonuclear reaction (1.2). As

well known, this process is caused by the giant resonance in the nuclear photoabsorption [18]. By now, there exist numerous reliable measurements of the cross sections $\sigma_{\gamma n}(k, Z, N)$ of the neutron γ production (1.2) for manifold nuclei. The respective data are put to use in our evaluations. The errors in these $\sigma_{\gamma n}$ measurements may rather amount ~ 10%, which puts a bound to the accuracy attainable in our evaluations. If anything, it is to point out that at the large converted γ -ray energies, $E_{\gamma} \gtrsim 30$ MeV, the contribution to (1.2) from area beyond the giant nuclear photoabsorption would be discernible because at these energies there exists the nuclear photoabsorption due to the surface absorption, the virtual quasi-deuteron absorption, and the absorption caused by the nucleon polarizability in nucleus [26]. Though this contribution ought to have been taken into account, its impact onto the quantities we have been considering were hardly more than a few per cent, even at $E_e(0) = 100$ MeV.

Absorption of the γ flux goes on inside sample in much the same way as in converter, yet l_C (1.18) gives place to $l_S(Z_S, \mathcal{N}_S, \rho_S, k)$ of the sample. Upon passing a distance y from the starting edge of sample (see Fig. 1), the γ flux (1.22) modifies as follows

$$J_{\gamma S}(y, k, R_C, Z_C, \rho_C, E_e^b, E_e^u, \Delta_e, t) = \\ = J_{\gamma C}(k, R_C, Z_C, \rho_C, E_E^b, E_e^u, \Delta_e, t) \exp[-\frac{y}{l_S(Z_S, \mathcal{N}_S, \rho_S, k)}].$$
(2.1)

Then the density of atoms $\mathcal{N}_{ris}(y, k, Z, N - 1, t)$ of the desirable radioisotope A'(Z, N - 1), produced per 1 s by the current density (2.1), with a given k, at the distance y (see Fig. 1) is determined by

$$\frac{\mathrm{d}\mathcal{N}_{\mathrm{ris}}(y,k,Z,N-1,t)}{\mathrm{d}t} = \\ = \mathcal{N}_{S}(Z,N) \cdot \sigma_{\gamma n}(k,Z,N) \cdot J_{\gamma S}(y,k,R_{C},Z_{C},\rho_{C},E_{e}^{b},E_{e}^{u},\Delta_{e},t), \quad (2.2)$$

where the density of sample atoms

$$\mathcal{N}_{S}(Z,N) = \frac{\rho_{S} \cdot 6.022 \cdot 10^{23}}{A_{S}}$$
(2.3)

is given in terms of the sample density ρ_S and the atomic weight A_S . When the isotope A(Z, N), needful to produce A'(Z, N - 1), constitutes only some part A_{bn} of the sample material, the density ρ_S in (2.3) is

$$\rho_S(Z,N) = \mathcal{A}_{bn}\bar{\rho}_S,\tag{2.4}$$

where $\bar{\rho}_S$ is the whole sample density, in particular the density of the natural element A_S . Unlike, the quantity l_S in Eq.(2.1) is determined by the total density $\bar{\rho}_S$ anyway.

Upon integrating the quantity (2.2) over the length of sample and over the photon energy k, we come to describe the total amount of radioisotope produced inside the sample, per 1 s, per 1 cm² of a sample area,

$$\frac{\mathrm{d}\mathcal{N}_{\mathrm{ris}}(Z,N-1,t)}{\mathrm{d}t} = J_e(t) \cdot \mathcal{N}_{\mathrm{ris}}^0(Z,N-1), \tag{2.5}$$

$$\mathcal{N}_{\mathrm{ris}}^{0}(Z, N-1) = \mathcal{N}_{S}(Z, N) \cdot \mathcal{N}_{C}(Z_{C}, N_{C}) \times \\ \times \int_{E_{e}^{b}}^{E_{e}^{u}} \mathrm{d}E\rho_{e}(E) \int_{0}^{R_{C}} \mathrm{d}x \int_{0}^{\infty} \mathrm{d}k \left(\frac{\mathrm{d}\sigma_{b}(k, E_{e}(x), Z_{C})}{\mathrm{d}k}\right) \sigma_{\gamma n}(k, Z, N) \times \\ \times \left(1 - \exp\left(-\frac{R_{S}}{l_{S}(k, Z_{S}, N_{S})}\right)\right) \cdot l_{S}(k, Z_{S}, N_{S}) \times \\ \times \exp\left(-\frac{R_{C} - x}{l_{C}(k, Z_{C}, N_{C})}\right). \quad (2.6)$$

The integration over the photon energy k is actually restricted by the area where the product

$$\left(\frac{\mathrm{d}\sigma_b(k)}{\mathrm{d}k}\right) \cdot \sigma_{\gamma n}(k) \tag{2.7}$$

has got a discernible value. Beyond any questions, the values $k \leq B_n$ and $k \geq E_e$ contribute just nothing into this integral over k into Eq. (2.6).

Expression (2.5) represents a source to produce this isotope A'(Z, N - 1). To proceed further, we are to recall that the produced radioisotope A'(Z, N - 1) is not stable, and its decay is governed by the lifetime τ_s , so that a number of decays per 1 s reads ordinarily

$$\frac{\mathcal{N}_{\mathrm{ris}}(t,\tau_s)}{\tau_s}.$$

Yet, the isotope A'(Z, N-1) itself undergoes irradiation by the same γ flux (2.1) as the original isotope A(Z, N) does. Then the photonuclear reaction

$$\gamma + A'(Z, N-1) \to A''(Z, N-2) + n$$
 (2.8)

results in depletion of the elaborated desired isotope A'(Z, N-1),

$$-\mathcal{N}_{\rm ris}(t,\tau_s)\frac{J_e(t)\,\mathcal{N}_{\rm ris}^0(Z,N-1)}{\mathcal{N}_S(Z,N)}.$$
(2.9)

Then, amenably to the common equation

$$\frac{\mathrm{d}\mathcal{N}_{\mathrm{ris}}(t,\tau_s)}{\mathrm{d}t} = J_e(t)\mathcal{N}_{\mathrm{ris}}^0(Z,N-1) - \frac{\mathcal{N}_{\mathrm{ris}}(t,\tau_s)}{\tau_s} - \mathcal{N}_{\mathrm{ris}}(t,\tau_s)\frac{J_e(t)\mathcal{N}_{\mathrm{ris}}^0(Z,N-1)}{\mathcal{N}_S(Z,N)}, \quad (2.10)$$

we obtain the radioisotope amount, per 1 cm^2 area of the sample, elaborated during an exposition time T_e

$$\mathcal{N}_{\rm ris}(T_e, \tau_s) = \mathcal{N}_{\rm ris}^0 \int_0^{T_e} \mathrm{d}t J_e(t) \exp[t/\tilde{\tau}_s] \cdot \exp[-T_e/\tilde{\tau}_s], \qquad (2.11)$$

$$\frac{1}{\tilde{\tau}_s(J_e(t))} = \frac{1}{\tau_s} + \frac{J_e(t) \mathcal{N}_{\rm ris}^0(Z, N-1)}{\mathcal{N}_S(Z, N)}.$$
(2.12)

Although, strictly speaking, the cross section $\sigma_{\gamma n}(k, Z, N)$ in the expression \mathcal{N}_{ris}^0 in Eq. (2.9), and in the last terms in Eqs. (2.10), (2.12) would give place to $\sigma_{\gamma n}(k, Z, N-1)$, we utilize here $\sigma_{\gamma n}(k, Z, N-1) \approx \sigma_{\gamma n}(k, Z, N)$ in the evaluations of these correction terms. For a time-independent initial electron current J_e , Eq. (2.11) reduces to

$$\mathcal{N}_{\rm ris}(T_e, \tau_s) = \mathcal{N}_{\rm ris}^0 J_e \tilde{\tau}_s (1 - \exp[-T_e/\tilde{\tau}_s]), \tag{2.13}$$

when $T_e \ll \tau_s$, it is simplified, giving just

$$\mathcal{N}_{\rm ris}(T_e, \tau_s) = \mathcal{N}_{\rm ris}^0 J_e T_e. \tag{2.14}$$

Let us mention that though the correction (2.9) is to be allowed for, its impact on the isotope production is very small, rather negligible, at the values of T_e , J_e currently treated.

It is to designate that we have been using, all over the carried out calculations, just the lifetime τ , yet not the so-called half-decay period $T_{1/2} = \tau \ln 2$.

It is generally accepted (see, for instance, [14-17, 27]) to describe the radioisotope production in terms of the yield $Y[Bq/(h \cdot \mu A \cdot mgA(Z, N))]$ of the produced activity in Bq per 1 h of exposition time, per 1 μ A of the initial electron current, and per 1 mg of the isotope A(Z, N) in the sample, which serves to produce the desirable isotope A'(Z, N - 1). Accordingly its definition, this characteristic Y is expressed through the quantity (2.11).

$$Y = \frac{\mathcal{N}_{\text{ris}}(Z, N-1, J_e, E_e^b, E_e^u, R_C, R_S, \mathcal{A}_{bn}, T_e, \tau_s)}{R_S(\text{cm}) \cdot \rho_S(\text{mg/cm}^3) A(Z, N) \cdot \tau_s(s) \cdot T_e(h) \cdot J_e(\mu A)}.$$
 (2.15)

It is also of use to discuss the total yield of activity produced by the initial electron current J_e inside the whole actual sample, with 1 cm² area and thickness R_S , during exposition time T_e

$$\mathcal{Y}(\mathbf{Bq}) = Y \cdot R_S(\mathbf{cm}) \cdot \bar{\rho}_S(\mathbf{mg/cm}^3) \cdot \mathcal{A}_{bn} \cdot J_e(\mu \mathbf{A}) \cdot T_e(\mathbf{h}).$$
(2.16)

Beside Y, \mathcal{Y} (2.15), (2.16), it is of value to consider the total amount of radioisotope A'(Z, N-1) elaborated in the whole sample

$$\mathcal{M}_{Z,N-1}(\mathbf{g}) = \frac{\mathcal{N}_{\mathrm{ris}}(Z,N-1,J_e,E_e^b,E_e^u,R_C,R_S,\mathcal{A}_{bn},T_e,\tau_s)\cdot\mathcal{A}_{bn}\cdot(Z+N-1)}{6.022\cdot10^{23}}, \quad (2.17)$$

where (Z + N - 1) = A - 1 is the corresponding atomic weight. In Secs. 3 and 4, we display the results of Y and \mathcal{M} evaluations. Apparently, a \mathcal{Y} value is directly expressed through a Y value accordingly (2.16).

Surely, besides the desirable isotope A'(Z, N-1) photoproduction (1.2), the reactions

$$A(Z, N) + \gamma = A'(Z, N-2) + 2n,$$
(2.18)

$$A(Z, N) + \gamma = A'(Z - 1, N) + p, \qquad (2.19)$$

$$A(Z,N) + \gamma = A'(Z-1,N-1) + p + n$$
(2.20)

are generally known to take place as well. Yet, their thresholds are nearly twice as much as the threshold of the reaction (1.2), and their cross sections are about ten times as small as the cross section of the reaction (1.2) [18]. So, with accuracy quite sufficient, the processes (2.18), (2.19), (2.20) are not competitive with the considered main photoproduction (1.2) of the isotope A'(Z, N-1). Surely, when desired, the yield of isotopes A'(Z, N-2), A'(Z-1, N-1), A'(Z-1, n) from irradiated sample would be calculated as well.

Let us recall that the eventual results (2.11)–(2.17) are governed by the manifold parameters, which characterize 1) the initial electron beam, $J_e, T_e, \bar{E}_e, E_e^b$, E_e^u, Δ_e ; 2) the converter, $\sigma_b, \mathcal{N}_C, \rho_C, R_C, l_C, K_C$; 3) the sample and the produced radioisotope, $\sigma_{\gamma n}, \mathcal{N}_S, \rho_S, Z_S, N_S, \mathcal{A}_{bn}, l_S, R_S, N, Z, \tau_s$. In involving these quantities into consideration, the proper discussions were explicated above. The dependence of $Y, \mathcal{M}, \mathcal{Y}$ on these parameters will be considered in Sec. 3 for some radioisotopes, produced immediately in the reaction (1.2). Thereafter, in Sec. 4, we inquire into the event that the decay

$$A'(Z, N-1) \Longrightarrow A^m(Z', N') \tag{2.21}$$

of this, at the first step obtained radioisotope A'(Z, N - 1) serves, in turn, as a source to produce the second-step radioisotope A^m , which is eventually put to use in manufacturing the needful practicable preparation.

3. EVALUATION OF THE RADIOISOTOPE PRODUCTION CHARACTERISTICS

Now we evaluate the quantities $Y, \mathcal{M}, \mathcal{Y}$, acquired above, for some examples, which typify the radioistope production using the electron beam. All over further consideration, the converter is presumed to be prepared of ^{nat}W (the natural tungsten) with a varying thickness $R_{\rm W}$ (cm), and three cases will be considered: the production of ⁹⁹Mo, ²³⁷U, ^{117m}Sn, with varying the sample thickness $R_{\rm Mo}$, $R_{\rm U}, R_{\rm Sn}$, the initial electron energy E_e and the current J_e , and the exposition time T_e . It is implied that we have been dealing with the average electron current provided by the electron linear accelerator or microtron. The purpose is to visualize the dependence of the production characteristics $Y, \mathcal{M}, \mathcal{Y}$ (2.15)–(2.17) on the aforesaid parameters.

First of all we treat the reaction

$$\gamma + {}^{100} \operatorname{Mo} \Longrightarrow {}^{99} \operatorname{Mo} + n \tag{3.1}$$

providing the production of the isotope ⁹⁹Mo, which is known to be the most applicable [4, 7], as discussed in Introduction. Let us recall the ⁹⁹Mo lifetime $\tau_{99Mo} \approx 96$ h.

As indicated by Eqs. (2.18), (2.19), (2.20), the isotopes ${}^{98}Mo$, ${}^{98}Nb$, ${}^{99}Nb$ could be recovered as well, if required.

In order to elucidate the key point of treatment, we display in Fig.2. the γ flux $J_{\gamma C}(k)$ (1.22) at the various thickness R_W of W converter and at the various initial electron energy (1.23). The behavior of $J_{\gamma C}(k)$ is to be correlated with the energy dependence of the cross section of the reaction (3.1) [28]. As understood, only the area of k values where $J_{\gamma C}$ and $\sigma_{\gamma n}$ overlap determines the evaluated quantities (2.5)–(2.17) to describe the radioisotope ⁹⁹Mo production, which we are treating now. The γ rays with energies k beyond this area are out of value. As the function $\sigma_{\gamma n}$ is well known to be, more or less, of the same form and magnitude for all the heavy and middle weight nuclei, Fig.2. typifies the calculation of radioisotope production by means of electron beam.

As explicated in the Sec. 1, the simultaneous treatment of both bremsstrahlung production and absorption and electron energy losses serves to realize how the isotope yield does depend on the converter thickness $R_{\rm W}$. This dependence is typified by Table 1. As understood there exists the most preferable $R_{\rm W}$ value for given material of the converter and the incident electron energy. In actual radioisotope manufacturing, just this R_C is to be utilized. Let us mention that the quantity $Y \approx 3.2 \text{ kBq/(h} \cdot \mu \text{A} \cdot \text{mg}^{100}\text{Mo})$ was obtained in [14] at $R_{\rm W} = 0.3 \text{ cm}$, which is some greater than the most preferable value $R_{\rm W} \approx 0.17 \text{ cm}$. As seen, the result of Y measurement in [14] does actually coincide with ours in Table 1, with a reasonable accuracy.

Table 1. The yield of activity $Y [\mathbf{kBq}/(\mathbf{h} \cdot \mu \mathbf{A} \cdot \mathbf{mg}^{100} \mathbf{Mo})]$ and amount $\mathcal{M} (10^{-2} \mathbf{mg})$ of 99 Mo at various converter thickness $R_W(\mathbf{cm})$, upon irradiating the natural ^{nat}Mo sample, with 1 cm² area and $R_{Mo} = 0.01$ cm (foil), by electrons with $E_e = 25$ MeV, $J_e = 1$ A/cm², during 1 h

$R_{\rm W}$	0.1	0.15	0.175	0.2	0.25	0.30
Y	3.63	4.09	4.07	3.99	3.80	3.62
\mathcal{M}	0.18	0.2	0.2	0.196	0.187	0.177

Table 2. The yield of activity $Y [\mathbf{kBq}/(\mathbf{h} \cdot \mu \mathbf{A} \cdot \mathbf{mg}^{100} \mathbf{Mo})]$ and amount $\mathcal{M} (10^{-2} \mathbf{mg})$ of the ⁹⁹Mo at various sample thickness $R_{Mo}(\mathbf{cm})$, upon irradiating the natural ^{nat}Mo sample during 1 h by electrons with $E_e = 25 \,\mathrm{MeV}$, $J_e = 1 \,\mathrm{A/cm^2}$, with the converter thickness $R_W = 0.15 \,\mathrm{cm}$

$R_{\rm Mo}$	0.01	0.5	1.0	1.5	2.0	4.0	6.0	8.0	10.0	12.0	14.0
Y	4.09	3.75	3.44	3.17	2.93	2.186	1.69	1.37	1.12	0.948	0.818
\mathcal{M}	0.2	9.2	16.8	23.4	28.65	42.9	49.73	53.3	55.0	56.2	56.8

Table 3. The same as in Table 2, yet for $R_W = 0.3$ cm, and for the initial electron energy distributed around $\bar{E}_e = 50$ MeV accordingly Eq. (1.23) with $E_e^b = 48.5$ MeV, $E_e^u = 52.5$ MeV, $\Delta_e = 0.5$ MeV

R_{Mo}	0.01	0.5	1.0	1.5	2.0	2.5
Y	11.73	10.73	9.86	9.07	8.37	7.78
\mathcal{M}	0.58	26.3	48.4	66.8	82.2	94.4

Table 4. The same as in Table 3, yet for $R_W = 0.4$ cm, and for the initial electron energy distributed around $\bar{E}_e = 100$ MeV accordingly Eq. (1.23) with $E_e^b = 95$ MeV, $E_e^u = 105$ MeV, $\Delta_e = 1$ MeV

R_{Mo}	0.01	0.5	1.0	1.5	2.0	2.5
Y	19.45	17.80	16.33	15.03	13.84	12.82
\mathcal{M}	0.95	43.7	80.1	110.6	136.1	157.2

The dependence of Y, \mathcal{M} on the R_S value at the various electron energies E_e gets understood from the data given in Tables 2, 3, 4. This Y, \mathcal{M} behaviour is due to the simultaneous run of the isotope ⁹⁹Mo photoproduction and the γ rays absorption in the Mo sample, as was acquired in Sec. 2. With R_{Mo} growing,

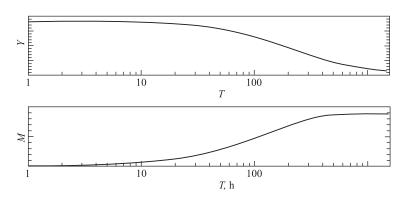


Fig. 3. Time dependence of the yield of activity $Y [\text{Bq/(h} \cdot \mu \text{A} \cdot \text{mg}^{100}\text{Mo})]$ and amount $\mathcal{M} (10^{-1} \text{ mg})$ obtained with the converter thickness $R_{\text{W}} = 0.3 \text{ cm}$ by irradiation of the natural ^{nat}Mo sample, with 1 cm² area and thickness $R_{\text{Mo}} = 0.01 \text{ cm}$ (foil), by electrons with $\bar{E}_e = 25 \text{ MeV}$, $J_e = 1 \text{ A/cm}^2$

the quantity N_{ris} (2.5), (2.11) increases substantially slower than linearly. That is why the quantity Y decreases, and M tends to some limit by increasing R_{Mo} .

The quantity \mathcal{Y} (2.16) behaves rather alike \mathcal{M} . With the same parameters, as in Table 3, for the natural ^{nat}Mo sample, $\rho_{Mo} = 9.8 \text{ g/cm}^3$, $\mathcal{A}_{bn} = 0.1$, with the thickness $R_{Mo} = 2 \text{ cm}$ and 1 cm^2 area, during 1 h exposition time, we have got

$$\mathcal{Y}_{^{99}\text{Mo}} \approx 1.7 \cdot 10^{10} \text{ kBq}, \tag{3.2}$$

which is rather noteworthy. If anything, by dividing the yield (2.16) on total sample mass, one might treat the so-called specific activity $\mathcal{Y}^{sp}_{_{99}Mo}$, which measures the activity of ⁹⁹Mo per unit mass of reaction products,

$$\mathcal{Y}_{^{99}\text{Mo}}^{sp} = \frac{\mathcal{Y}_{^{99}\text{Mo}}}{\rho_{^{99}\text{Mo}} \cdot R_{^{99}\text{Mo}} \cdot 1 \text{ cm}^2} \approx 10^9 \,\frac{\text{kBq}}{\text{g}}.$$
(3.3)

Yet this quantity would be rather of small use, as it does actually depend on the sample and converter parameters, $R_C, R_S, Z_C, Z_S, \rho_C, \rho_S$, the exposition time T_e , the percentage \mathcal{A}_{bn} of ¹⁰⁰Mo in the sample, and so on. That is why we have been making use of $\mathcal{Y}_{^{99}Mo}$ itself without having recourse to $\mathcal{Y}_{^{99}Mo}^{sp}$ (3.3).

Figure 3 offers the time dependence of the quantities Y (2.15) and \mathcal{M} (2.17). They represent the produced activity and mass as a function of exposition time T_e in hours. With T_e increasing, the quantity \mathcal{N}_{ris} grows tangibly slower than linearly. Consequently, $Y(T_e)$ decreases and $\mathcal{M}(T_e)$ tends to a finite limit when T_e increases. As seen, there is no reason for too long exposition time.

Table 5 demonstrates how the quantities R_W, Y , and \mathcal{M} depend on the initial electron energy. As seen, the most preferable R_W value increases smoothly with

Table 5. The yield of activity $Y [kBq/(h \cdot \mu A \cdot mg^{100}Mo)]$ and amount $\mathcal{M} (10^{-2} mg)$ of ⁹⁹Mo at various initial electron energy distributions described by \bar{E}_e , E_e^b , E_e^u , Δ_e , all in MeV, as given in Eq. (1.23), and at the most preferable respective thicknesses $R_{\rm W}(\rm cm)$. The natural ^{nat}Mo sample, with the thickness $R_{\rm M0} = 0.01$ cm and 1 cm² area, is irradiated by the electron current $J_e = 1A/\rm{cm}^2$, during 1 h

\bar{E}_e	20	25	50	100
E_e^b	19.5	24.5	48.5	95
E_e^u	20.5	25.5	52.5	105
Δ_e	0.2	0.2	0.5	1.0
$R_{\rm W}$	0.1	0.180	0.3	0.4
Y	2.0	4.09	11.73	19.45
\mathcal{M}	0.1	0.2	0.58	0.95

electron energy growth. The feature to emphasize is the sharp augmentation of Y, \mathcal{M} in coming from $\bar{E}_e = 20$ MeV to $\bar{E}_e = 25$ MeV and then to $\bar{E}_e = 50$ MeV, yet the relatively slower enhancement shows up by increasing \bar{E}_e from $\bar{E}_e = 50$ MeV to $\bar{E}_e = 100$ MeV.

The next example of considerable practical interest [29] is the photoproduction of the tin isomer radioisotope 117m Sn

$$\gamma + {}^{118}\operatorname{Sn} \Longrightarrow {}^{117m}\operatorname{Sn} + n. \tag{3.4}$$

We put to use the cross section of this reaction acquired from [30]. The results of Y (2.15) and \mathcal{M} (2.17) evaluation are presented in Table 6 for various initial electron energies and for various thicknesses $R_{\rm W}$ and $R_{\rm Sn}$ of the W converter and of the natural tin ^{nat}Sn sample, with 1 cm² area. Let us recall that the isotope ¹¹⁸Sn constitutes about 24% of the natural tin, that is $\mathcal{A}_{bn} \approx 0.24$ in (2.4), $\bar{\rho}_{\rm Sn} =$ 7 g/cm³, and the isomer ^{117m}Sn lifetime $\tau_{117\rm Sn} \approx 20.2$ d [24]. As seen, Table 6 offers the same dependence of Y (2.15) and \mathcal{M} (2.17) on the electron energy for the ^{117m}Sn production, as Table 5 for the production of ⁹⁹Mo does. Accordingly to the data in Table 6, the quantity \mathcal{Y} (2.16) at $\bar{E}_e = 50$ MeV, $R_{\rm Sn} = 2$ cm proves to be

$$\mathcal{Y}_{^{117m}\mathrm{Sn}} \approx 0.8 \cdot 10^{10} \mathrm{\,kBq},\tag{3.5}$$

which is of the same order, as the \mathcal{Y} (3.2) for ⁹⁹Mo production.

At last, we discuss the production of the widely applied [31], specifically in the nuclear fuel research, radioisotope 237 U,

$$\gamma + {}^{238}\mathrm{U} \Longrightarrow {}^{237}\mathrm{U} + n. \tag{3.6}$$

\bar{E}_e	20	25	50	100
E_e^b	19.5	24.5	48.5	95
E_e^u	20.5	25.5	52.5	105
Δ_e	0.2	0.2	0.5	1.0
$R_{ m W}$	0.1	0.15	0.3	0.4
$Y, R_{\rm Sn} = 0.01$	0.456	1.04	3.18	5.48
$Y, R_{\rm Sn} = 2.0$	0.34	0.78	2.37	4.08
$\mathcal{M}, R_{\mathrm{Sn}} = 0.01$	0.27	0.62	1.89	3.26
$\mathcal{M}, R_{\mathrm{Sn}} = 2.0$	40.84	93.00	283.6	487.5

Table 6. The same as in Table 5, yet here the quantities $Y [kBq/(h \cdot \mu A \cdot mg^{118}Sn)]$ and $\mathcal{M}(10^{-2} mg)$ are obtained for $^{117}Sn^m$ production from the natural tin ^{nat}Sn sample, with the thicknesses $R_{Sn} = 0.01$ cm (foil), $R_{Sn} = 2$ cm, and 1 cm² area

Table 7. The same as in Table 6, yet the quantities $Y [kBq/(h \cdot \mu A \cdot mg^{238}U)]$ and $\mathcal{M} (10^{-2} mg)$ are obtained for ^{237}U produced from the natural ^{nat}U

\bar{E}_e	20	25	50	100
E_e^b	19.5	24.5	48.5	95
E_e^u	20.5	25.5	52.5	105
Δ_e	0.1	0.1	0.5	1.0
$R_{ m W}$	0.15	0.20	0.35	0.45
$Y, R_{\rm U} = 0.01$	1.01	1.77	4.08	6.64
$Y, R_{\rm U} = 2.0$	0.45	0.78	1.78	2.89
$\mathcal{M}, R_{\rm U} = 0.01$	6.3	11.07	25.44	41.41
$\mathcal{M}, R_{\rm U} = 2.0$	558.4	978.9	2234	3626

The cross section of this reaction is acquired from [32]. All the consideration runs in much the same way as in the cases of treating the ⁹⁹Mo and ^{117m}Sn production. Yet now we evaluate the quantities Y (2.15), \mathcal{M} (2.17) not just at the time T_e , the finish of the exposition, but in one day after the 5 h-long irradiation. The reason to do so is that the experimental measurements of the ²³⁷U production were carried out in [15] just under such conditions. Apparently, as the time of observation T, counting from the start of irradiation, is longer than the exposition time T_e , the quantities (2.15), (2.17) are to be replaced by

$$Y(T) = Y(T_e) \exp\left[-(T - T_e)/\tau_{237} \mathrm{U}\right], \tag{3.7}$$

$$\mathcal{M}(T) = \mathcal{M}(T_e) \exp\left[-(T - T_e)/\tau_{237_{\rm U}}\right],\tag{3.8}$$

with the ²³⁷U lifetime $\tau_{^{237}\text{U}} = 6.75\text{d}$, $T - T_e = 1\text{d}$, which are presented in Table 7. For the parameters utilized in [15], $R_W = 0.3 \text{ cm}$, $\bar{E}_e = 24 \text{ MeV}$, $\Delta_e \rightarrow 0$, we have got $Y_U \approx 1.35 \text{ kBq}/(\text{h} \cdot \mu \text{A} \cdot \text{mg}^{238}\text{U})$, which is in accordance with the result obtained in [15], $Y_U \approx 1.1 \text{ kBq}/(\text{h} \cdot \mu \text{A} \cdot \text{mg}^{238}\text{U})$. Let us recall the isotope ²³⁸U constitutes 99.276% of the natural U, that is $\mathcal{A}_{bn} \approx 1$ in (2.4), (2.16), (2.17), and $\rho_U = 18.7 \text{ g/cm}^3$. Then, utilizing the data from Table 7, and choosing $\bar{E}_e = 50 \text{ MeV}$, $R_U = 2 \text{ cm}$, $T_e = 5 \text{ h}$ (unlike the cases of ⁹⁹Mo,^{177m} Sn), T = 30 h, the quantity \mathcal{Y} (2.16) proves to be

$$\mathcal{Y}_{^{237}\mathrm{U}} \approx 35 \cdot 10^{10} \,\mathrm{kBq},\tag{3.9}$$

that is still more significant than the \mathcal{Y} values for ⁹⁹Mo and ¹¹⁷Sn, (3.2), (3.5).

4. PRODUCTION OF A PRACTICABE RADIOISOTOPE VIA AN ISOTOPE-PRECURSOR

In a number of important cases, a radioisotope of practical use $A^m(Z', N')$ is generated by decaying

$$A'(Z, N-1) \Longrightarrow A^m(Z', N') + e^{\pm}$$
(4.1)

an isotope A'(Z, N-1) obtained in the photonuclear reaction (1.2), which was described in previous Sec. 3. Thus, the parent isotope decay (4.1) is now a source to produce a needful eventual radioisotope $A^m(Z', N')$ with a lifetime τ_m . The density of atoms \mathcal{N}_{ris}^m of this isotope A^m produced by the γ flux (2.1) inside a given sample is then described by the common equation

$$\frac{\mathrm{d}\mathcal{N}_{\mathrm{ris}}^m(t,\tau_s,\tau_m)}{\mathrm{d}t} = p_m \frac{\mathcal{N}_{\mathrm{ris}}(t,\tau_s)}{\tau_s} - \frac{\mathcal{N}_{\mathrm{ris}}^m(t,\tau_s,\tau_m)}{\tau_m} \,. \tag{4.2}$$

Here p_m stands to allow for the fact that the isotope decay (4.1) constitutes a share p_m of all the possible decays of A(Z, N-1). Amenably Eq. (4.2), we generally obtain the amount of radioisotope $A^m(Z', N')$ for the sample with 1 cm² area, at the total time T, counting from the exposition start,

$$\mathcal{N}_{\mathrm{ris}}^{m}(T,\tau_{s},\tau_{m}) = p_{m} \frac{\exp[-T/\tau_{m}]}{\tau_{s}} \int_{0}^{T} \mathrm{d}t \exp[t/\tau_{m}] \mathcal{N}_{\mathrm{ris}}(t,\tau_{s}), \qquad (4.3)$$

with the quantity $\mathcal{N}_{ris}(t, \tau_s)$ given by Eqs. (2.10)–(2.14). Ordinarily, we are dealing with the practicable case $T \geq T_e$. In calculating \mathcal{N}_{ris}^m (4.3), we have abandoned leaking the isotope $A^m(Z', N')$ due to the feasible photonuclear reaction $A^m(Z', N')(\gamma, n)A''(Z', N'-1)$ during exposition time T_e . In the case a constant initial electron current J_e irradiates converter during the exposition time T_e , and afterwards disappears, the general Eq. (4.3) reduces to

$$\mathcal{N}_{\mathrm{ris}}^{m}(T, T_{e}, \tau_{s}, \tau_{m}) = \\ = \mathcal{N}_{\mathrm{ris}}^{0} J_{e} p_{m} \frac{\tilde{\tau}_{s}}{\tau_{s}} \left(\exp\left[-\frac{T}{\tau_{m}}\right] \left(\tau_{m} \left(\exp\left[\frac{T_{e}}{\tau_{m}}\right] - 1\right) - \tau_{-} \left(\exp\left[\frac{T_{e}}{\tau_{-}}\right] - 1\right) + \right. \\ \left. + \tau_{-} \left(1 - \exp\left[-\frac{T_{e}}{\tilde{\tau}_{s}}\right]\right) \left(\exp\left[\frac{T}{\tau_{-}}\right] - \exp\left[\frac{T_{e}}{\tau_{-}}\right]\right) \right) \right), \quad (4.4) \\ \left. \frac{1}{\tau_{-}} = \frac{1}{\tau_{m}} - \frac{1}{\tilde{\tau}_{s}}.$$

With replacing the quantity $\mathcal{N}_{ris}(T_e, \tau_s)$ in Eqs. (2.15)–(2.17) by $\mathcal{N}_{ris}^m(T, T_e, \tau_s, \tau_m)$ (4.3), (4.4), and τ_s by τ_m as well, the quantities Y^m and \mathcal{M}^m are defined to describe the eventual isotope $A^m(Z', N')$ production.

Hereafter, using Eq. (4.4), we treat the production of the most extensively employed radioisotope 99m Tc [4,7], which stems in the 99 Mo β decay

$$^{99}\text{Mo} \longrightarrow {}^{99m}\text{Tc} + e^-.$$
 (4.5)

The branching of the β decay of ⁹⁹Mo into the isomer ^{99m}Tc, with the lifetime $\tau_m \approx 10$ h, amounts $\approx 85\%$, that is $p_m \approx 0.85$ in Eq. (4.4) [33]. In other cases ⁹⁹Mo decays giving the practically stable ⁹⁹Tc isotope with $\tau_{\rm Tc} \approx 4 \cdot 10^5$ y [14, 24, 33]. All the results presented hereafter are obtained for the Mo sample of 1 cm² area, as had been doing in the previous Secs. 1–3.

Tables 8,9 show that for a given T_e there exists the most preferable time T_{\max} , counting from the exposition start, when the yield of 99m Tc activity Y_{Tc^m} and the mass $\mathcal{M}_{\text{Tc}^m}$ have got their maxima. Therefore the radioisotope 99m Tc is to be extracted out of the Mo sample upon the time T_{\max} best of all. This fact is thought to be of a practical value, though the dependence of Y_{Tc^m} and $\mathcal{M}_{\text{Tc}^m}$ yield on T sees to be rather smooth.

Table 10 shows the activity yield Y_{Tc^m} decreases and the mass $\mathcal{M}_{\text{Tc}^m}$ tends to a certain limit as the thickness R_{Mo} of Mo sample increases. That is so because the quantity $\mathcal{N}_{\text{ris}}^m$ (4.3) increases substantially slower than linearly, just alike the quantity \mathcal{N}_{ris} (2.11) does.

Tables 11, 12 figure the quantities $Y_{Tc^m}(T)$, $\mathcal{M}_{Tc^m}(T)$ calculated at $T = T_e$ and $T = T_{max}$, for the various initial electron energies \overline{E}_e (attached by the associated parameters E_e^b , E_e^u , Δ_e as in Table 5), with choosing the most

Table 8. The time $T_{\max}(\mathbf{h})$ of maximum accumulation of the isotope 99m Tc and the respective yield of activity $Y [\mathbf{kBq}/(\mathbf{h} \cdot \mu \mathbf{A} \cdot \mathbf{mg}^{100}\mathbf{Mo})]$ and amount $\mathcal{M}_{\mathbf{Tc}^m}(10^{-5} \, \mathbf{mg})$, as functions on the time $T_e(\mathbf{h})$ of irradiation of the natural ^{nat}Mo sample, with 1 cm² area and $R_{\mathbf{Mo}} = 0.01$ cm (foil), by electrons with $J_e = 1 \, \mathbf{A}/\mathbf{cm}^2$, $\bar{E}_e = 25$ MeV, at the converter thickness $R_{\mathrm{W}} = 0.3$ cm

T_e	0.5	1	5	10	15	20
$T_{\rm max}$	20	23	25	28	30	32
Y_{Tc^m}	2.54	2.52	2.44	2.32	2.21	2.15
$\mathcal{M}_{\mathrm{Tc}^m}$	5.65	11.3	54.3	103	147	188

Table 9. The T(h) dependence of the yield of activity $Y_{\text{Tc}^m}[\text{kBq}/(\text{h} \cdot \mu \text{A} \cdot \text{mg}^{100}\text{Mo})]$ and amount $\mathcal{M}_{\text{Tc}_m}(10^{-5} \text{ mg})$ of ^{99m}Tc which results inside the natural ^{nat}Mo sample, with 1 cm² area and the thickness $R_{\text{Mo}} = 0.01$ cm (foil), irradiated during $T_e = 0.5$ h by electrons with $\bar{E}_e = 25$ MeV, $J_e = 1$ A/cm²; the converter thickness $R_{\text{W}} = 0.3$ cm

T	0.5	1.5	5.0	10	20	30	40	50	60	80	100
Y_{Tc^m}	0.092	0.434	1.43	2.07	2.54	2.50	2.32	2.11	1.9	1.55	1.26
$\mathcal{M}_{\mathrm{Tc}^m}$	0.2	0.96	3.19	4.60	5.65	5.56	5.16	4.70	4.24	3.44	2.79

Table 10. The dependence of the yield of 99m Tc activity $Y_{\text{Tc}^m}[\text{kBq}/(\text{h} \cdot \mu \text{A} \cdot \text{mg}^{100}\text{Mo})]$ and amount $\mathcal{M}_{\text{Tc}^m}(10^{-5} \text{ mg})$ on the thickness $R_{\text{Mo}}[\text{cm}]$ of the natural ^{nat}Mo sample, with 1 cm² area, irradiated during $T_e = 0.5$ h by electrons with $J_e = 1 \text{ A/cm}^2$, $\bar{E}_e = 25$ MeV. The converter thickness $R_{\text{W}} = 0.3$ cm. All the results are obtained at the time T = 20 h, counting from exposition start

$R_{\rm Mo}$	0.01	0.5	1	2	4	6	8	10	12	16	20
Y_{Tc^m}	2.54	2.30	2.13	1.80	1.36	1.05	0.84	0.7	0.59	0.45	0.36
$\mathcal{M}_{\mathrm{Tc}^m}$	5.65	264	478	810	1209	1405	1502	1549	1573	1590	1595

preferable values of the converter thickness $R_{\rm W}$ and the time $T_{\rm max}$ for each \bar{E}_e . It is of interest to correlate the results obtained for the Mo foil, $R_{\rm Mo} = 0.01$ cm, with those for the thick enough Mo sample, $R_{\rm Mo} = 2$ cm. Just for that matter, the evaluation firstly carried out at $R_{\rm Mo} = 0.01$ cm is then replicated at $R_{\rm Mo} = 2$ cm, with the results offered in Tables 11 and 12, respectively.

Accordingly the data in Table 12, the radioisotope production characteristic \mathcal{Y} (2.16), the total yield of 99m Tc activity, at $\bar{E}_e = 50$ MeV is found to be

$$\mathcal{Y}_{\mathrm{Tc}^{m}}(T_{\mathrm{max}}) \approx 1.2 \cdot 10^{10} \,\mathrm{kBq}\,,\tag{4.6}$$

Table 11. The yield of activity $Y_{\text{Te}^m}[\mathbf{kBq}/(\mathbf{h} \cdot \mu \mathbf{A} \cdot \mathbf{mg}^{100} \mathbf{Mo})]$ and amount $\mathcal{M}_{\text{Te}^m}(10^{-5} \text{ mg})$ of 99m Tc, evaluated at $T = T_e(\mathbf{h})$ and $T = T_{\max}(\mathbf{h})$, the most preferable time of 99m Tc extraction, for various initial electron energies $\bar{E}_e(\text{MeV})$. The natural ^{nat}Mo sample, with 1 cm² area and the thickness $R_{\text{Mo}} = 0.01$ cm (foil), is irradiated during $T_e = 1$ h by the current $J_e = 1$ A/cm². R_{W} is the converter thickness, preferable at the given \bar{E}_e

\bar{E}_e	20	25	50	100
$R_{ m W}$	0.1	0.15	0.3	0.4
T_{\max}	23	23	23.5	24
$Y_{\mathrm{Tc}^{m}}(T_{e})$	0.1	0.2	0.59	0.99
$Y_{\mathrm{Tc}^m}(T_{\mathrm{max}})$	1.42	2.88	8.28	13.92
$\mathcal{M}_{\mathrm{Tc}^m}(T_e)$	0.45	0.91	2.62	4.4
$\mathcal{M}_{\mathrm{Tc}^m}(T_{\mathrm{max}})$	6.29	12.79	36.8	61.82

Table 12. The same as in Table 11, yet with $R_{Mo} = 2 \text{ cm}$

\bar{E}_e	20	25	50	100
$R_{ m W}$	0.1	0.15	0.3	0.4
T_{\max}	23	23	23.5	24
$Y_{\mathrm{Tc}^{m}}(T_{e})$	0.07	0.15	0.42	0.71
$Y_{\mathrm{Tc}^m}(T_{\mathrm{max}})$	1.02	2.06	5.90	9.91
$\mathcal{M}_{\mathrm{Tc}^m}(T_e)$	66.4	134	383	643
$\mathcal{M}_{\mathrm{Tc}^m}(T_{\mathrm{max}})$	922	1858	5328	8941

that is of the same order as the corresponding value (3.2) for ⁹⁹Mo. In other words, let one irradiate the natural ^{nat}Mo sample, with the 1 cm² area and the thickness $R_{\rm Mo} = 2$ cm, during $T_e = 1$ h by the γ flux originated by the electron beam, with $\bar{E}_e = 50$ MeV and $J_e = 1$ A/cm², in the ^{nat}W converter with the thickness $R_{\rm W} = 0.3$ cm. Then, the ⁹⁹Mo activity (3.2) would be elaborated by the end of exposition, and, in turn, the ^{99m}Tc activity (4.6), comparable with (3.2), would be generated at the time $T_{\rm max} = 23.5$ h

It is to mention that upon extracting the isotope 99m Tc out of the Mo sample at $T = T_{\rm max}$, the next amount of 99m Tc isotope, comparable with that at $T = T_{\rm max}$, would be accumulated in the Mo sample in $T_1 \approx \tau_{{}^{99m}\text{Tc}} \ln(\tau_{{}^{99}\text{Mo}}/\tau_{{}^{99m}\text{Tc}}) \approx 23$ h, as can be realized from Eq. (4.4). Yet further repeatedly, over and over again, withdrawing 99m Tc out of the sample is usually thought to be rather of less efficiency because of diminishing the 99 Mo amount.

Of course, the examples treated in the presented work do not cover all the area of the radioisotope application in these days. In particular, there exists a number of practicable isotopes eligible to be wrought up by the method described hereupon, in the photonuclear reactions such as

$$\gamma + {}^{124}\text{Xe} \Longrightarrow {}^{123}\text{I} + n ,$$

$$\gamma + {}^{237}\text{Np} \Longrightarrow {}^{236m}\text{Np} + n ,$$

and so on [6, 16]. Further investigations in this way are believed to be carried out before long.

Aforesaid obtaining 99m Tc out of 99 Mo typifies manufacturing the practicable radioisotope due to decay of some preceding isotope, procured at the first step, in the photonuclear reaction (1.2).

The values of Y, \mathcal{Y} , \mathcal{M} acquired in Secs. 3, 4 are believed to be of practical interest, which is discussed next. Let us here recollect that accuracy of our findings is at all the points about $\sim 10\%$, as was explicated at every stage in carrying out the presented calculations.

5. FINDINGS CONSIDERATION

Once, for all we have by now acquired, there emerge alluring prospects of the radioisotopes photoproduction around electron linear accelerators.

Hereafter we correlate and contrast salient features of the routine reactorbased radioisotope production, even though with the conversion from the HEUto LEU-targets, and the electron accelerator-based radioisotope production, addressing advantages of the last, specifically with respect to the case of recovery of ⁹⁹Mo and ^{99m}Tc, which are by far the major medical isotopes salable and consumed to-day [4, 7, 9, 10]. We follow the timely industry convention, and quantify the radioisotope production and supply in terms of *6-day curies per week* [7, 9, 10], which is nominally the quantity of ⁹⁹Mo activity remaining 6 days after the recovered ⁹⁹Mo leaves the producer's facility, provided the ⁹⁹Mo has been elaborated during one week, and then was refined and processed before shipment to the market.

Let the electron beam with $J[A/cm^2]$ and $\bar{E}_e = 50 \text{ MeV}$ (see Fig. 1.) irradiate the tungsten converter with $R_W = 0.3 \text{ cm}$, and the γ flux, converted from this electron beam, produce the isotope Mo⁹⁹ in the Mo sample, with $R_{Mo} = 2 \text{ cm}$ and 1 cm² area, amenably to the photonuclear reaction (3.1). Then, with allowance for the time-dependence of Y (2.15), Y (2.16), \mathcal{M} (2.17) (see Fig. 3), and the data given by Tables 2, 3, we infer that the total yield of activity by the end of exposition would be

$$\mathcal{Y}(T_e, J_e, \mathcal{A}_{bn}) = J_e \cdot T_e \cdot \mathcal{A}_{nb} \cdot 1.7 \cdot 10^{11} \,\mathrm{kBq} \approx 5 \cdot 10^3 \cdot J_e \cdot T_e \cdot \mathcal{A}_{bn} \,\mathrm{Ci}, \tag{5.1}$$

provided the exposition time $T_e \lesssim 15$ h. At $T_e = 1$ h and $J_e = 1$ A/cm², we have got the value (3.2) given above. The accelerator can be turned on and off at will and without any consequences, and exchanging the irradiated targets is rather a simple thing, which are apparent advantages of the accelerator-based radioisotope production over the routine reactor-based one. So we are in position of irradiating a set of Mo targets successively, one after the other with the exposition time of each one equal to the most efficient value $T_e \approx 15$ h. Then, the yield of activity produced in every one of those samples is

$$\mathcal{Y}(15h, J_e, \mathcal{A}_{bn}) \approx 5 \cdot 10^3 \cdot J_e \cdot 15 \cdot \mathcal{A}_{nb} \operatorname{Ci.}$$
 (5.2)

As understood, this way leads to the greatest yield of activity generally attainable during a total given exposition time. Let us irradiate in this manner a set of ten samples so that the total exposition time consumed in one week constitutes ≈ 150 h. That series of ten targets expositions results in the total yield of activity per one week

$$\mathcal{Y}(10 \times 15 \text{ h}, J_e, \mathcal{A}_{bn}) \approx 5 \cdot 10^3 \cdot J_e \cdot 15 \times 10 \cdot \mathcal{A}_{nb} \text{ Ci.}$$
 (5.3)

As observed, this total activity is accumulated in the separated samples, taken together. On the other hand, we can continually irradiate one single sample one week long, i.e., again for ≈ 150 h. In this case the evaluation accordingly Secs. 3, 4 (Fig. 3, Table 3) results in the total yield of activity accumulated per one week in that single target

$$\mathcal{Y}(150 \text{ h}, J_e, \mathcal{A}_{bn}) \approx 3.2 \cdot 10^3 \cdot J_e \cdot 150 \cdot \mathcal{A}_{nb} \text{ Ci}, \tag{5.4}$$

which shows up to be noticeably smaller than the quantity (5.3). Let us opt a realizable value $J_e = 10 \text{mA/cm}^2$, and presume that we operate targets composed of the pure isotope 100 Mo, i.e., $A_{bn} = 1$ in the expressions (5.1)–(5.4). Then we arrive at

$$\mathcal{Y}(10 \times 15 \text{ h}, 10 \text{ mA}, 1) \approx 7.5 \cdot 10^3 \text{Ci},$$
 (5.5)

$$\mathcal{Y}(150 \text{ h}, 10 \text{ mA}, 1) \approx 4.8 \cdot 10^3 \text{Ci.}$$
 (5.6)

Recalling $\tau_{99M0} = 96$ h, the aforesaid *6-day curies* corresponding to the quantities (5.5), (5.6) are directly evaluated

$$\mathcal{Y}_{6-day}(10 \times 15 \text{ h}, 10 \text{ mA}, 1) \approx 1.67 \cdot 10^3 \text{Ci},$$
 (5.7)

$$\mathcal{Y}_{6-day}(150 \text{ h}, 10 \text{ mA}, 1) \approx 1.07 \cdot 10^3 \text{Ci.}$$
 (5.8)

These quantities (5.5)–(5.8) evaluated with practicable ¹⁰⁰Mo targets and a realizable electron beam prove to be competitive with the marketable *large-scale* productivity of the *large-scale producers*, who supply more than 1000 *6-day* *curies* of ⁹⁹Mo *per week* to the market on the routine reactor basis, with operating HEU targets [7].

Nowadays, the pure laboratory study [14–17] of the processes (3.1), (3.4), (3.6), with using foils of natural Mo, Sn, U as irradiated targets, have blazed the trail towards *the large-scale* radioisotope manufacturing based on the electron-accelerator driving photoneutron nuclear reactions.

In reactor-based radioisotope producing, no matter whether the HEU- or LEUtarget is used, the quantity of ⁹⁹Mo available for sale and harnessing is much less than the total quantity of ⁹⁹Mo produced in an irradiated target because of this 6-day delay and, primarily, because of losses caused by the very sophisticated and time-consuming target processing, still before shipment to the market. Upon irradiating and then cooling, the targets are processed into hot cells facilities, which can cost as much as tens of millions of dollars to construct, and which are very sophisticated to operate [7,11]. The point is to recover a thoroughly purified desired radioisotope (for instance ⁹⁹Mo) out of a target where this constitutes, at best, a few per cent among ²³⁵U fission fragments [34]. In particular, the isotope 99 Mo, several hours after a moment of fission, constitutes $\sim 6\%$ of fission fragments. The other way round, in the accelerator-based photoneutron production, there requires no hot-sells and subsidiary equipment for targets processing after the end of exposition, as a matter of fact. As well, the desired isotope, e.g., ⁹⁹Mo, is immediately elaborated within a pure molibdenium target, so that there is no need to purify anything and manage any wastes. Therefore the aforesaid 6-day term for calibrating activity of the shipment (6-day curies) is to be recounted just from the end of target exposition.

Used ether HEU- or LEU-target, one of the most important issues to take care of is anyway to eliminate, or at least to minimize, the weapon-usable waste streams resulting from radioisotope production. In particular concern is that little or no progress is being made for now in this way. Only a very small fraction, typically about 3%, of the 235 U in a target undergoes fission in reactor-based radioisotope, e.g., 99 Mo, producing [7, 11]. The vast majority of the uranium in the target, along with other fission products and target materials, are eventually treated as wastes, no matter whether the HEU- or LEU-target is used. Tens of kilograms of HEU wastes are annually accumulated worldwide. By contrast, the electron-accelerator-based radioisotope production has nothing to do with any radioactive wastes, there is no waste stream at all, in actual fact.

The decay product of ⁹⁹Mo, the isotope ^{99m}Tc (see Sec. 4), we are primarily focused on, is used in about two-thirds of all the diagnostic and therapeutic nuclear-medical procedures all over the world [5, 9, 11, 12]. The metastable radioisotope ^{99m}Tc having got the short lifetime, the ⁹⁹Mo recovered out of an irradiated target is shipped to radiopharmacies and hospitals within the *technetium generators* that are *eluted* to obtain the desired ^{99m}Tc at destinations. The calibration to asses *Tc-generator* activity is based on the number of curies that are contained in a *generator* on the day of, or the day after its delivery to a user [4, 7, 11]. In the considered photoneutron radioisotope production, an irradiated Mo target could be processed in the *Tc generator* just after the end of exposition, which is again an evident advantage over the routine reactor-based production, as the last requires a considerable time and work to prepare that irradiated HEU- or LEU-target for usage in the *Tc generator*. Of course, the appropriate required *Tc generator* is anew to be designed and built for recovering ^{99m}Tc from an irradiated Mo sample, upon photoproducing the ⁹⁹Mo radioisotope therein, instead of the routine *Tc generator* to process the blend of different Mo isotopes extracted out of ²³⁵U fission fragments. The findings explicated in Sec. 4 will serve for all these actual purposes. The methods how to recover the Tc from Mo irradiated targets are by now elaborated as well [8, 36].

As readily understood [7], refurbishing the obsolent reactors and converting from HEU-based to LEU-based radioisotope production would be anyway time consuming, at least 5–6 years long, and technically sophisticated, at least not less than to bring online the accelerator-based radioisotope production. Along with other complexities, the conversion would anew require the very expensive construction of the special *hot-cells* for processing now the LEU-targets, which are not involved at all into the accelerator-based photoneutron radioisotope production.

In the routine radioisotope reactor-based elaboration, there is a very long implicated and vulnerable supply chain of manifold operations, beginning with the HEU provision of targets producers and terminating in treating an end-user. Any contingency in a single link results in a fatal malfunction of all the chain, all the more that diverse operations are performed at different sites, in different countries, and even at different continents. In contrast, radioisotope photoneutron production would be accomplished at one single site: from an unsophisticated target preparation straightforwardly to radiopharmaceutical manufactures, or, as, e.g., in the ⁹⁹Mo production case, to charging the *Tc generator*. There is no issue of shipment of the ⁹⁹Mo product to the ^{99m}Tc generator manufacturing facilities. The losses of radioisotope yield caused by decay rate would be then minimized, and even almost eliminated, by co-locating all the engaged facilities. Under such circumstances, any irradiated ¹⁰⁰Mo target, upon utilizing by Tc generator, would be restored, and then exposed anew. A circle of this kind could many times be repeated which would allow saving the stick of starting enriched material, as, e.g., the ¹⁰⁰Mo isotope in producing the ⁹⁹Mo isotope. That agenda would offer the possibility of self-contained generator systems being feasible for central radiopharmaceutical labs for a grope of hospitals. So, for all we have acquired, there offers a new stream from ⁹⁹Mo production to an end-user consumption of kits prepared with 99m Tc.

As understood, see Sec.3, the nuclear photoneutron process $A(Z,N)(\gamma,n)A'(z,N-1)$ can serve to produce the great variety of desired

radioisotopes, not only with $A \sim 100$, $A \sim 140$, i.e., not only with A placed within the humps of mass distribution of uranium fission fragments. Especially, it is to indicate the isotope 201 Tl, that is thought to replace 99 Mo/ 99m Tc usage, and a number of specific radioisotopes used in the positron emission tomography (PET), 13 N, 18 F, 82 Sr/ 82 Rb, 45 Ti, 60 Cu, and so on [35], which are not available in the uranium fission process.

The above discussions are leading to consideration of building new and operating to-day existing electron linear accelerators (e-linacs) for the radioisotope production. As understood, see Eqs. (5.1)–(5.8), the for now deployed 1/2MW e-linac TRIUMF [11,37], with electron energy $E_e = 50$ MeV and current density $J_e = 10$ mA/cm² can be considered to be eligible for manufacturing 1000 *6-day curies* ⁹⁹Mo *activity per week*, i.e., for the *large scale* ⁹⁹Mo production. So, a single machine of this kind could manufacture and supply the ⁹⁹Mo marketable quantity comparable to productivity of a single *large scale* producer, provided the required ¹⁰⁰Mo pure targets are available. The manifold efficient methods and technologies to separate various isotopes are by now developed and deployed, see, e.g., [6, 8]. So, recovery of a pure singe-isotope target, e.g., the pure ¹⁰⁰Mo isotope target, is believed to be not over-expensive, when the *large scale* radioisotope photoneutron manufacture would be validated.

Laboratories around the world, such as TRIUMPF (Canada), BNL, ORNL (U.S.), IRN-Orseay, GANIL (France), ELBE (Deutshland) [37-39], have expertise and facilities that can be used immediately. The construction of far more powerful e-linacs, with $E_e = 50 \text{ MeV}, J_e = 100 \text{mA/cm}^2$, are by now under way, and they are believed to be commissioned before long, in 3-4 years, which would underpin a long-term enhancement of desired radioisotopes production [11]. The estimated cost of such new accelerator is about \$50 millions, whereas the cost of a research and test reactor, with the thermal neutron flux $\approx (10^{14} - 10^{15})$ n/(s · cm²), is assessed to be at least \$300-\$400 millions. For instance, construction cost for the new 100MW reactor in Cadarache (France) is estimated to be about 500 millions of euros [7]. Just fixing the MAPLE reactors would have cost tens of millions of dollars, whereas building such new reactor or refurbishing NRU would have cost hundreds of millions of dollars. Even 5-years license extension for NRU would have required expenditure of about hundred of millions of dollars [7, 11]. Similarly, the reactor operations are far more costly than the e-linac operations. Power consumption, dominating the operating costs, is roughly estimated to be a few MWs for an aforesaid e-linac, and the total operating costs are assessed to constitute about 10% of the capital investment. Such an accelerator facility, as treated above, would be viewed as a single-purposed facility operating strictly for radioisotope production business.

The γ flux, converted from electron beam of an electron accelerator, can also be used for the photofission of ²³⁸U, utilizing the natural or depleted uranium targets, with subsequent recovering the desired radioisotope, e.g., ⁹⁹Mo, from the

fission fragments blend [11]. The heretofore treated photoneutron production of radioisotopes is certain to be far more efficient and viable than the radioisotope recovery out of the fission fragments of the ²³⁸U photofission. In order to grasp the reason one is first to recollect that cross sections $\sigma_{\gamma n}$ of the reaction (1.2) are akin the cross section $\sigma_{\gamma f}$ of the 238 U photofission, both being of the same order [40]. Target nuclear densities are of the same order as well. Yet the desired radioisotope, e.g., ⁹⁹Mo, constitutes at best only a few per cent, never more than $\sim (5-6)\%$, among ²³⁸U photofission fragments. Thus, given the γ flux causing both reactions is the same, the yield of photoneutron reaction proves to be far more abundant than one from processing the irradiated ²³⁸U sample upon the ²³⁸U photofission. Anyway, the anew target processing and generator-manufacturing facilities are to be deployed, in using both photoproduction, ${}^{100}Mo(\gamma, n){}^{99}Mo$, and photofission ${}^{238}U$ process, ${}^{238}U(\gamma, F)$. Yet although by this ${}^{99}Mo$ photofission production, just alike in the photoneutron process, the accelerator does not produce radioactive waste from its operation, the waste from the irradiated targets chemical processing to recover, extract and purify ⁹⁹Mo would be similar to the waste of the reactor-based production. The ⁹⁹Mo recovery from ²³⁸U photofission fragments and from ²³⁵U thermal-neutron fission fragments are actually analogous. In either methods, the capital investments emerge to be very high, as the special facilities, in particular the hot-sells, are required to deal with the emission and disposal of highly radioactive fission products. In contrast, in the radioisotope photoneutron production, there are neither uranium fission fragments to deal with, nor radioactive wastes at all. Treated photoneutron radioisotope producing, there occur no secondary transuranic nuclei, in particular ²³⁹Pu, associated with radioisotope producing based on the ²³⁸U photofission. As understood, see Eqs. (5.1)-(5.8), the mass of about 20g of 100% enriched ¹⁰⁰Mo is quite sufficient to design a practicable target for the large-scale ⁹⁹Mo photoneutron production, whereas a depleted ²³⁸U target for the photofission radioisotope production would require the mass of at least $\sim 200g$ [11]. This large target mass is a substantial challenge in procuring required purity of the obtained medical radioisotopes. Contamination possibility of a produced radioisotope, e.g., ⁹⁹Mo, even increases due to the much larger mass of the photofission ²³⁸U target as compared to the mass of the ²³⁵U target in the case of the thermal neutron fission. So, as it has been coming to light, the photoneutron production techniques has got a lot of advantages over the photofission one. Surely, it is least of all to say that these two approaches rule each other out. They are naturally to complement each other to procure the most reliable radioisotope supply.

Further calculations and laboratory measurements are required to verify and validate the proof-of-principles that have been treated in the work presented.

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