

ОБЪЕДИНЕННЫЙ ИНСТИТУТ ЯДЕРНЫХ ИССЛЕДОВАНИЙ

Дубна

E2-2001-16

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THRESHOLD EFFECTS IN INCLUSIVE τ-LEPTON DECAY

Submitted to the XV International Seminar on High Energy Physics Problems «Relativistic Nuclear Physics and Quantum Chromodynamics», September 25–29, 2000, Dubna, Russia

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1. A theoretical and experimental study of processes at a low energy scale is very important in QCD because it allows one to investigate effects lying beyond the framework of the perturbative approach. At present, there is rich experimental material obtained from hadronic τ -lepton decays. The first theoretical analysis of hadronic decays of a heavy lepton was performed in 1971 [1] before the experimental discovery of the τ -lepton in 1975. Since then, the properties of the τ have been studied very intensively.

In this talk we discuss the well-known ratio of hadronic to leptonic widths for the inclusive decay of the τ -lepton, R_{τ} , which now known experimentally with high precision. This ratio serves for extracting of the values of the QCD running coupling α_S at the τ mass scale and the QCD parameter Λ [2].

The initial theoretical expression for R_{τ} contains an integral over timelike momentum

$$R_{\tau} = \frac{2}{\pi} \int_{0}^{M_{\tau}^{2}} \frac{ds}{M_{\tau}^{2}} \left(1 - \frac{s}{M_{\tau}^{2}}\right)^{2} \left(1 + 2\frac{s}{M_{\tau}^{2}}\right) \operatorname{Im} \Pi(s) , \qquad (1)$$

which extends down to small s and cannot be directly calculated in the framework of the standard perturbation theory (PT). Indeed, the hadronic correlator $\Pi(s)$ is parametrized by the perturbative running coupling that has unphysical singularities and, therefore, is ill-defined in the region of small momenta. To avoid this problem, one usually applies the following procedure. The initial integral (1) is rewritten by using the Cauchy theorem in the form of a contour integral in the complex plane with the contour running around a circle with radius M_{τ}^2 [3, 4]:

$$R_{\tau} = \frac{1}{2\pi i} \oint_{|z|=M_{\tau}^2} \frac{dz}{z} \left(1 - \frac{z}{M_{\tau}^2}\right)^3 \left(1 + \frac{z}{M_{\tau}^2}\right) D(z), \qquad (2)$$

where $D(z) = -z \ d\Pi(z)/dz$ is the Adler function [5]. This trick allows one, in principle, to avoid the problem of a direct calculation of the R_{τ} ratio. However, it should be noted that in order to perform this transformation self-consistently, it is necessary to maintain correct analytic properties of the hadronic correlator, which are violated in the framework of standard PT. The analytic approach in QCD [6] (see also [7, 8]), which we will use here, maintains needed analytic properties and allows one to perform self-consistently the procedure of analytic continuation.

We begin by representing the R_{τ} -ratio in the form

$$R_{\tau} = R_{\tau}^{0} (1 + \delta_{\text{QCD}}), \tag{3}$$

where R_{τ}^0 corresponds to the parton level description and $\delta_{\rm QCD}$ is the QCD correction. Also, we introduce QCD contributions to the imaginary part of the hadronic correlator, r(s), and to the corresponding Adler function, d(z): $\mathcal{R}(s) = [{\rm Im} \ \Pi(s+i\epsilon)/\pi]/R_{\tau}^0 \propto 1 + r$, $D \propto 1 + d$. Then, one can write $\delta_{\rm QCD}$ as an integral over timelike momentum (Minkowskian region)

$$\delta_{\text{QCD}} = 2 \int_0^{M_\tau^2} \frac{ds}{M_\tau^2} \left(1 - \frac{s}{M_\tau^2} \right)^2 \left(1 + 2 \frac{s}{M_\tau^2} \right) r(s) , \qquad (4)$$

or as a contour integral in the complex plane (Euclidean region)

$$\delta_{\text{QCD}} = \frac{1}{2\pi} \oint_{|z|=M_2^2} \frac{dz}{z} \left(1 - \frac{z}{M_\tau^2} \right)^3 \left(1 + \frac{z}{M_\tau^2} \right) d(z) \,. \tag{5}$$

2. The PT description is based on the contour representation and can be developed in the following two ways. In the Braaten's (Br) method [3] the quantity (5) is represented in the form of truncated power series with the expansion $a_{\tau} = \alpha_S(M_{\tau}^2)/\pi$. In this case the three-loop representation for $\delta_{\rm QCD}$ is

$$\delta_{\text{QCD}}^{\text{Br}} = a_{\tau} + r_1 a_{\tau}^2 + r_2 a_{\tau}^3 \,, \tag{6}$$

where the coefficients r_1 and r_2 in the $\overline{\text{MS}}$ scheme with three active flavors are $r_1 = 5.2023$ and $r_2 = 26.366$ [3].

The method proposed by Le Diberder and Pich (LP) [4] uses the PT expansion of the d-function

$$d(z) = a(z) + d_1 a^2(z) + d_2 a^3(z), (7)$$

where in the $\overline{\rm MS}$ -scheme $d_1^{\overline{\rm MS}}=1.6398$ and $d_2^{\overline{\rm MS}}=6.3710$ [9] for three active quarks. The PT running coupling a(z) is obtained from the renormalization group equation with the three-loop β -function.

The substitution of Eq. (7) into Eq. (5) leads to the following non-power representation

$$\delta_{\text{QCD}}^{\text{LP}} = A^{(1)}(a) + d_1 A^{(2)}(a) + d_2 A^{(2)}(a)$$
(8)

with

$$A^{(n)}(a) = \frac{1}{2\pi i} \oint_{|z|=M_x^2} \frac{dz}{z} \left(1 - \frac{z}{M_\tau^2}\right)^3 \left(1 + \frac{z}{M_\tau^2}\right) a^n(z). \tag{9}$$

As noted above, transformation to the contour representation (5) requires the existence of certain analytic properties of the correlator: namely, it must be an analytic function in the complex z-plane with a cut along the positive real axis. The correlator parametrized, as usual, by the PT running coupling does not have this virtue. Moreover, the conventional renormalization group method determines the running coupling in the spacelike region, whereas the initial expression (1) contains an integration over timelike momentum, and there is the question of how to parametrize a quantity defined for timelike momentum transfers [10]. To perform this procedure self-consistently, it is important also to maintain correct analytic properties of the hadronic correlator [11, 12, 13]. Because of this failure of analyticity, Eqs. (4) and (5) are not equivalent in the framework of PT and, if one remains within PT, it is difficult to estimate the errors introduced by this transformation. However, using the analytic theory of perturbation (APT) approach, it is possible to resolve these problems.¹

3. In the framework of the analytic approach, the functions d(z) and r(s) are expressed in terms of the effective spectral function $\rho(\sigma)$ [6, 12]

$$d(z) = \frac{1}{\pi} \int_0^\infty \frac{d\sigma}{\sigma - z} \, \rho(\sigma) \,, \qquad r(s) = \frac{1}{\pi} \int_s^\infty \frac{d\sigma}{\sigma} \rho(\sigma) \,. \tag{10}$$

The spectral function is defined as the imaginary part of the perturbative² approximation to $d_{\rm pt}(z)$ on the physical cut. At the three-loop level, it is

$$\rho(\sigma) = \varrho_0(\sigma) + d_1 \varrho_1(\sigma) + d_2 \varrho_2(\sigma), \qquad \varrho_n(\sigma) = \operatorname{Im}[a_{\operatorname{pt}}^{n+1}(\sigma + i\epsilon)]. \tag{11}$$

¹The nonperturbative a-expansion technique in QCD [14] also leads to a well-defined procedure of analytic continuation [11].

²To distinguish APT and PT cases, we will use subscripts "an" and "pt".

The function $\varrho_0(\sigma)$ in Eq. (11) defines the analytic spacelike, $a_{\rm an}(z)$, and timelike (s-channel), $\tilde{a}_s(s)$, running couplings:

$$a_{\rm an}(z) = \frac{1}{\pi} \int_0^\infty \frac{d\sigma}{\sigma - z} \, \varrho_0(\sigma) \,, \qquad \tilde{a}_s(s) = \frac{1}{\pi} \int_s^\infty \frac{d\sigma}{\sigma} \, \varrho_0(\sigma).$$
 (12)

As has been argued from general principles, the behavior of these couplings cannot be the same [15]. It should be stressed that, unlike the PT running coupling, the analytic running coupling has no unphysical ghost pole and, therefore, possesses the correct analytic properties, arising from Källén-Lehmann analyticity reflecting the general principles of the theory. For example, one-loop APT result is [6, 12]³

$$a_{\rm an}^{(1)}(z) = a_{\rm pt}^{(1)}(z) + \frac{4}{\beta_0} \frac{\Lambda^2}{\Lambda^2 + z}, \quad \tilde{a}_{\rm an}^{(1)}(s) = \frac{4}{\beta_0} \left[\frac{1}{2} - \frac{1}{\pi} \arctan \frac{\ln(s/\Lambda^2)}{\pi} \right], \quad (13)$$

where
$$a_{\rm pt}^{(1)}(z) = \frac{4}{\beta_0 \ln(-z/\Lambda^2)}$$
 and $\beta_0 = 9$.

Using Eq. (4) or equivalently Eq. (5), we obtain the QCD correction to the R_{τ} -ratio in terms of $\rho(\sigma)$ as follows

$$\delta_{\rm an} = \frac{1}{\pi} \int_{M_{\tau}^2}^{\infty} \frac{d\sigma}{\sigma} \rho(\sigma) + \frac{1}{\pi} \int_0^{M_{\tau}^2} \frac{d\sigma}{\sigma} \left[2 \frac{\sigma}{M_{\tau}^2} - 2 \left(\frac{\sigma}{M_{\tau}^2} \right)^3 + \left(\frac{\sigma}{M_{\tau}^2} \right)^4 \right] \rho(\sigma) \,. \tag{14}$$

This expression can be presented as the non-power expansion, which looks like the Eq. (8): $\delta_{\rm an} = \delta_{\rm an}^{(0)} + d_1 \, \delta_{\rm an}^{(1)} + d_2 \, \delta_{\rm an}^{(2)}$.

The difference between the PT (LP) and APT contributions to the R_{τ} can be transparently shown by the one-loop relation:

$$\delta_{\rm an}^{(1)} = \delta_{\rm pt}^{(1)} - \frac{8}{\beta_0} \frac{\Lambda^2}{M_\tau^2} + \mathcal{O}(\Lambda^4/M_\tau^4) \,. \tag{15}$$

The additional term, which is 'invisible' in the perturbative expansion, turns out to be important numerically [18, 19]. Due to the negative sign of this term $\Lambda_{\rm an} > \Lambda_{\rm pt}$ at the same value of the QCD correction: $\delta_{\rm an}(\Lambda_{\rm an}) = \delta_{\rm pt}(\Lambda_{\rm pt}) = \delta^{ext}$.

In the case of massless quarks, the APT analysis of the inclusive τ decay at the three-loop level has been performed in [20]. In Table 1 we compare this result with the perturbative calculations performed by Braaten's and Le Diberder–Pich methods. This table demonstrates that the APT expansion has much improved convergence properties as compared with different PT approximations. The investigation [20] (see also [7, 21, 22]) allow us to formulate the following features of the APT method: (i) this approach maintains the correct analytic properties and leads to a self-consistent procedure of analytic continuation from the spacelike to the timelike region; (ii) it has much improved convergence properties and turns out to be stable with respect to higher-loop corrections; (iii) renormalization scheme dependence of the results obtained within this method is reduced dramatically.

In studying a relationship between theoretical predictions and experimental data, it is important to connect measured quantities with "simplest" theoretical objects to

³The analytic running couplings (the exact two-loop and the three-loop after an approximation) can be written explicitly in the term of the Lambert function [16, 17].

Table 1: Relative contributions of higher-loop terms in different methods.

Method	Expansion terms
APT	$1 + \delta_{\rm an} = 1 + 0.167 + 0.021 + 0.002$
PT (LP)	$1 + \delta_{\text{pt}}^{\text{LP}} = 1 + 0.148 + 0.030 + 0.012$
PT (Br)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

check direct consequences of the theory without using model assumptions in an essential manner. Some single-argument functions which are directly connected with experimentally measured quantities can play the role of these objects. A theoretical description of inclusive processes can be made in terms of functions of this sort. Among them there is the Adler D-function that can be extracted from the experimental data in the process of e^+e^- annihilation into hadrons and the inclusive decay of the τ lepton.

4. The R_{τ} -ratio can be separated experimentally in the form of three parts

$$R_{\tau} = R_{\tau,V} + R_{\tau,A} + R_{\tau,S}. \tag{16}$$

The terms $R_{\tau,V}$ and $R_{\tau,A}$ are contributions coming from the non-strange hadronic decays associated with vector (V) and axial-vector (A) quark currents respectively, and $R_{\tau,S}$ contains strange decays (S).

Within the perturbative approximation with massless quarks the vector and axial-vector contributions to R_{τ} coincide with each other

$$R_{\tau,V} = R_{\tau,A} = \frac{3}{2} |V_{ud}|^2 (1 + \delta_{QCD}),$$
 (17)

where $|V_{ud}|$ denotes the CKM matrix element. However, the experimental measurements [23, 24] shown that these components are not equal to each other. The corresponding difference is associated with non-perturbative QCD effects which are usually described in the form of power corrections [3, 23, 24]. The experimental data for the isovector spectral function [23, 24] have been used in [25] to extract the Adler D_V -function which we show as the dashed line in Fig. 1. The experimental D-function turns out to be a smooth function without any traces of resonance structure. One can expect that this object more precisely reflects the quark-hadron duality and, therefore, is convenient for comparing theoretical predictions with experimental data. Note here that any finite order of the operator product expansion fails to describe the infrared tail of the D-function. We will apply the analytic approach and study the role of quark masses and threshold effects by comparing our results with experimental data for the light Adler function corresponding to the non-strange vector channel of τ decay data. This function defined in the Euclidean region is a convenient proving ground to test theoretical methods.

⁴The *D*-function obtained in [26] from the data for electron-positron annihilation into hadrons has a similar property.

⁵The Minkowskian and Euclidean characteristics of the process of electron-positron annihilation into hadrons have been considered in [27].

5. To incorporate effects connected with quark masses for the process of the τ decay occurring by the vector current via $W^- \to \bar{u}d$, we take the approximation from [28, 29], which can be written as follows

$$\mathcal{R}(s) = T(v) [1 + g(v)r(s)] \Theta(s - 4m^2), \qquad (18)$$

where

$$T(v) = v \frac{3 - v^2}{2}, \ g(v) = \frac{4\pi}{3} \left[\frac{\pi}{2v} - \frac{3 + v}{4} \left(\frac{\pi}{2} - \frac{3}{4\pi} \right) \right], \ v = \sqrt{1 - \frac{4m^2}{s}}, \tag{19}$$

and $m = m_u = m_d$ denotes the effective mass of u and d quarks which we take here to be equal each other.

Further, we take into account, that the region of integration in Eq. (1) includes the vicinity of the quark-antiquark threshold. The perturbative expansion breaks down in this vicinity due to singularities at $s=(m_q+m_{\bar q})^2$ [28, 29]. Thus any finite order of perturbative expansion is unreliable near quark threshold and, therefore, all singular terms of the $(\alpha_S/v)^n$ type have to be summarized. Note, this problem cannot be avoided, if instead of Eq. (1) one uses the contour representation (2), because these expressions should be equivalent to each other in the framework of a systematic method. For heavy quark systems one usually uses the nonrelativistic resummation factor obtained by using the Schrödinger equation with the Coulomb potential, which is known as the Sommerfeld-Sakharov factor [30, 31]. For systematic description of the threshold region in the system of light quarks it is essential from the very beginning to have a relativistic generalization of this factor. Moreover, it is important to take into account the difference between the Coulomb potential in the case of QED and the quark-antiquark potential in the case of QCD. This QCD relativistic factor has been proposed in [32] to have the form

$$S(\chi) = \frac{X(\chi)}{1 - \exp\left[-X(\chi)\right]}, \qquad X(\chi) = \frac{4\pi \alpha_S}{3 \sinh \chi}, \tag{20}$$

where χ is the rapidity which related to s by $2m \cosh \chi = \sqrt{s}$. The relativistic resummation factor (20) reproduces both the expected nonrelativistic and ultrarelativistic limits and corresponds to a QCD-like quark-antiquark potential.

The threshold resummation factor leads to the following modification of the expression (18)

$$\mathcal{R}_V(s) = T(v) \left[S(\chi) - \frac{1}{2} X(\chi) + g(v) r(s) \right] \Theta(s - 4m^2), \qquad (21)$$

which we use to calculate the vector part of R_{τ}

$$R_{\tau,V} = 3S_{\text{EW}}|V_{ud}|^2 \int_0^{M_\tau^2} \frac{ds}{M_\tau^2} \left(1 - \frac{s}{M_\tau^2}\right)^2 \left(1 + \frac{2s}{M_\tau^2}\right) \mathcal{R}_V(s), \qquad (22)$$

where $S_{\rm EW}$ denotes the electroweak factor [3].

By using a dispersion relation for the hadronic correlator, the Adler function corresponding to the non-strange vector current can be represented as

$$D_V(Q^2) = Q^2 \int_0^\infty ds \, \frac{\mathcal{R}_V(s)}{(s+Q^2)^2} \,. \tag{23}$$

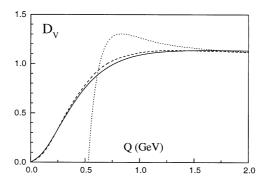


Figure 1: The vector D-function for the τ decay. The solid curve is the APT result. The experimental curve (dashed line) corresponding to the ALEPH data and the perturbative result with power corrections (dotted line) are taken from [25].

In Fig. 1 we plot the D-function obtained in the APT approach (solid curve) by using the value of the quark masses $m_u = m_d = 250 \,\mathrm{MeV}$. Practically the same value of the light quark masses were used in [33, 34]. These values are close to the constituent quark masses and incorporate some nonperturbative effects. The shape of the infrared tail of the D-function is sensitive to the value of these masses. We use $\Lambda = 400 \,\mathrm{MeV}$ in the $\overline{\mathrm{MS}}$ and obtain the value of $R_{\tau,V} = 1.76$ which agrees well with the experimental data presented by the ALEPH, $R_{\tau,V}^{\mathrm{expt}} = 1.775 \pm 0.017$ [23], and the OPAL, $R_{\tau,V}^{\mathrm{expt}} = 1.764 \pm 0.016$ [24], Collaborations. The experimental curve (dashed line) and the curve which corresponds to the perturbative result with power corrections (dotted line) are taken from [25].

6. We have presented the description of the 'light' vector D-function based on the analytic approach in QCD which is not in conflict with the general principles of the theory. The conventional method approximating this function as a sum of perturbative terms and power corrections cannot describe the low energy scale region. We have shown that within the APT approach, taking into account mass and threshold effects, it is possible to obtain good agreement with experimental data down to the lowest energy scale. Moreover, we have found that threshold resummation is very important for the problem considered here. The effect of the QCD relativistic S-factor is a reduction of the value of the QCD scale parameter Λ extracted from the τ -data, which turned out to be too large within the massless analysis [20] compared with high-energy data. Thus, our analysis demonstrates the important role played in τ -lepton physics by both the analytic properties and the threshold resummation.

We would like to thank D.V. Shirkov and A.N. Sissakian for interest in this work. Partial support of the work by the US National Science Foundation, grant PHY-9600421, and by the US Department of Energy, grant DE-FG-03-98ER41066, and by the RFBR, grants 99-01-00091, 99-02-17727, 00-15-96691 is gratefully acknowledged.

References

- [1] Y.S. Tsai, Phys. Rev. **D4**, 2821 (1971).
- [2] Particle Data Group, C. Caso et al., Eur. Phys. C3, 1 (1998); D.E. Groom et al., Eur. Phys. C15, 1 (2000).
- [3] E. Braaten, Phys. Rev. Lett. 60, 1606 (1988); Phys. Rev. 39, 1458 (1989);
 E. Braaten, S. Narison and A. Pich, Nucl. Phys. B373, 581 (1992).
- [4] F. Le Diberder and A. Pich, Phys. Lett. **B286**, 147 (1992).
- [5] S.L. Adler, Phys. Rev. **D10**, 3714 (1974).
- [6] D.V. Shirkov and I.L. Solovtsov, JINR Rap. Comm. 2[76], 1996, hep-ph/9604363;Phys. Rev. Lett. 79, 1209 (1997).
- [7] K.A. Milton, I.L. Solovtsov and O.P. Solovtsova, in: Proceedings the XXIX Int. Conf. on High Energy Physics, Vancouver, B.C., Canada, July 23-29, 1998, vol. II, 1608.
- [8] I.L. Solovtsov and D.V. Shirkov, Theor. Math. Phys. 120, 1220 (1999).
- [9] S.G. Gorishny, A.L. Kataev and S.A. Larin, Phys. Lett. **B259**, 144 (1991).
- [10] A.V. Radyushkin, Preprint JINR, E2-82-159 (1982);
 N.V. Krasnikov and A.A. Pivovarov, Phys. Lett. 116B, 168 (1982).
- [11] H.F. Jones and I.L. Solovtsov, Phys. Lett. B 349, 519 (1995); in: Proceedings of Int. Eur. Conference on High Energy Physics, eds. J. Lemonne et al., Brussels, 27 July-2 August, 1995.
- [12] K.A. Milton and I.L. Solovtsov, Phys. Rev. **D55**, 5295 (1997);
 K.A. Milton and O.P. Solovtsova, Phys. Rev. **D57**, 5402 (1998).
- [13] D.V. Shirkov, Preprint JINR-E2-2000-211, hep-ph/0009106 v.2, Preprint JINR-E2-2000-298, hep-ph/0012283.
- [14] I.L. Solovtsov, Phys. Lett. **B327**, 335 (1994); Phys. Lett. **B340**, 245 (1994).
- [15] K.A. Milton and I.L. Solovtsov, Phys. Rev. D59, 107701 (1999).
- [16] B. Magradze, in: Proceedings of the XX Int. Seminar "QUARKs-98", Suzdal, Russia, May 17-24, 1998, eds. F.L. Bezrukov et. al., Moscow, 1999, hep-ph/9808247; Int. J. of Mod. Phys. A15, 2715 (2000); Preprint JINR E2-2000-222, hep-ph/0010070.
- [17] E. Gardi, G. Grunberg and M. Karliner, JHEP **07**, 007 (1998).
- [18] O.P. Solovtsova, JETP Lett. **64**, 714 (1996).
- [19] K.A. Milton, I.L. Solovtsov and O.P. Solovtsova, Phys. Lett. **B415**, 104 (1997).

- [20] K.A. Milton, I.L. Solovtsov, O.P. Solovtsova, and V.I. Yasnov, Eur. Phys. J. C14, 495 (2000).
- [21] I.L. Solovtsov and D.V. Shirkov, Phys. Lett. B442, 344 (1998); Theor. Math. Phys. 120, 1220 (1999).
- [22] D.V. Shirkov, Theor. Math. Phys. 119, 438 (1999), hep-th/9810246.
- [23] ALEPH Collaboration, R. Barate et al., Eur. Phys. J. C4, 409 (1998); Z. Phys. C76, 15 (1997).
- [24] OPAL Collaboration, K. Ackerstaff et al., Eur. Phys. J. C7, 571 (1999).
- [25] S. Peris, M. Perrottet and E. de Rafael, JHEP 05, 011 (1998); hep-ph/9805442.
- [26] S. Eidelman, F. Jegerlehner, A.L. Kataev, and O. Veretin, Phys. Lett. B454, 369 (1999).
- [27] K.A. Milton, I.L. Solovtsov and O.P. Solovtsova, Eur. Phys. J. C13, 497 (2000).
- [28] T. Appelquist and H.D. Politzer, Phys. Rev. Lett. 34, 43 (1975); Phys. Rev. D12, 1404 (1975).
- [29] E.C. Poggio, H.R. Quinn and S. Weinberg, Phys. Rev. **D13**, 1958 (1976).
- [30] A. Sommerfeld, Atombau und Spektrallinien, vol. II (Vieweg, Braunschweig, 1939).
- [31] A.D. Sakharov, Sov. Phys. JETP 18, 631 (1948).
- [32] K. A. Milton and I. L. Solovtsov, Preprint OKHEP-00-06, hep-ph/0005175.
- [33] A.I. Sanda, Phys. Rev. Lett. 42, 1658 (1979).
- [34] I.L. Solovtsov and D.V. Shirkov, in: Proceedings of the Int. Workshop on " e^+e^- collisions: from ϕ to J/Ψ ", Novosibirsk, Russia, 1999, hep-ph/9906495.

Received by Publishing Department on February 5, 2001 В рамках аналитической теории возмущения, которая позволяет разрешить проблему нефизических особенностей типа призрачного полюса и дать самосогласованное описание процессов в пространственно- и во времениподобной областях, проведен анализ инклюзивного распада τ -лептона в адроны с учетом пороговых эффектов. Пороговое поведение кварк-антикварковой системы описано с помощью нового релятивистского фактора, суммирующего особенности пертурбативного разложения типа $(\alpha_S/v)^n$. Показано, что пороговые эффекты приводят к уменьшению параметра Λ , извлекаемого из данных по τ -распаду, а также что предложенный метод приводит к результату, который хорошо согласуется с экспериментальными данными для функции Адлера в векторном канале вплоть до самых низких энергий.

Работа выполнена в Лаборатории теоретической физики им. Н.Н.Боголюбова ОИЯИ.

Препринт Объединенного института ядерных исследований. Дубна, 2001

Milton K.A., Solovtsov I.L., Solovtsova O.P. Threshold Effects in Inclusive τ -Lepton Decay

E2-2001-16

Within the framework of the analytic perturbation theory, which allows one to resolve the problem of unphysical singularities, like the ghost pole, and gives a self-consistent description of both space-like and time-like regions, the inclusive decay of the τ -lepton is analyzed taking into account threshold effects. The threshold behavior of a quark-antiquark system is described by using the new relativistic factor, summing singularities of the perturbative expansion of the $(\alpha_S/v)^n$ type. It is shown that threshold effects reduce a value of the parameter Λ extracted from the τ -decay data and that the method proposed leads to a good agreement with experimental data for the vector Adler function down to the lowest energy scale.

The investigation has been performed at the Bogoliubov Laboratory of Theoretical Physics, JINR.

Preprint of the Joint Institute for Nuclear Research. Dubna, 2001

Макет Т.Е.Попеко

Подписано в печать 11.03.2001 Формат $60 \times 90/16$. Офсетная печать. Уч.-изд. листов 1,04 Тираж 425. Заказ 52536. Цена 1 р. 25 к.

Издательский отдел Объединенного института ядерных исследований Дубна Московской области